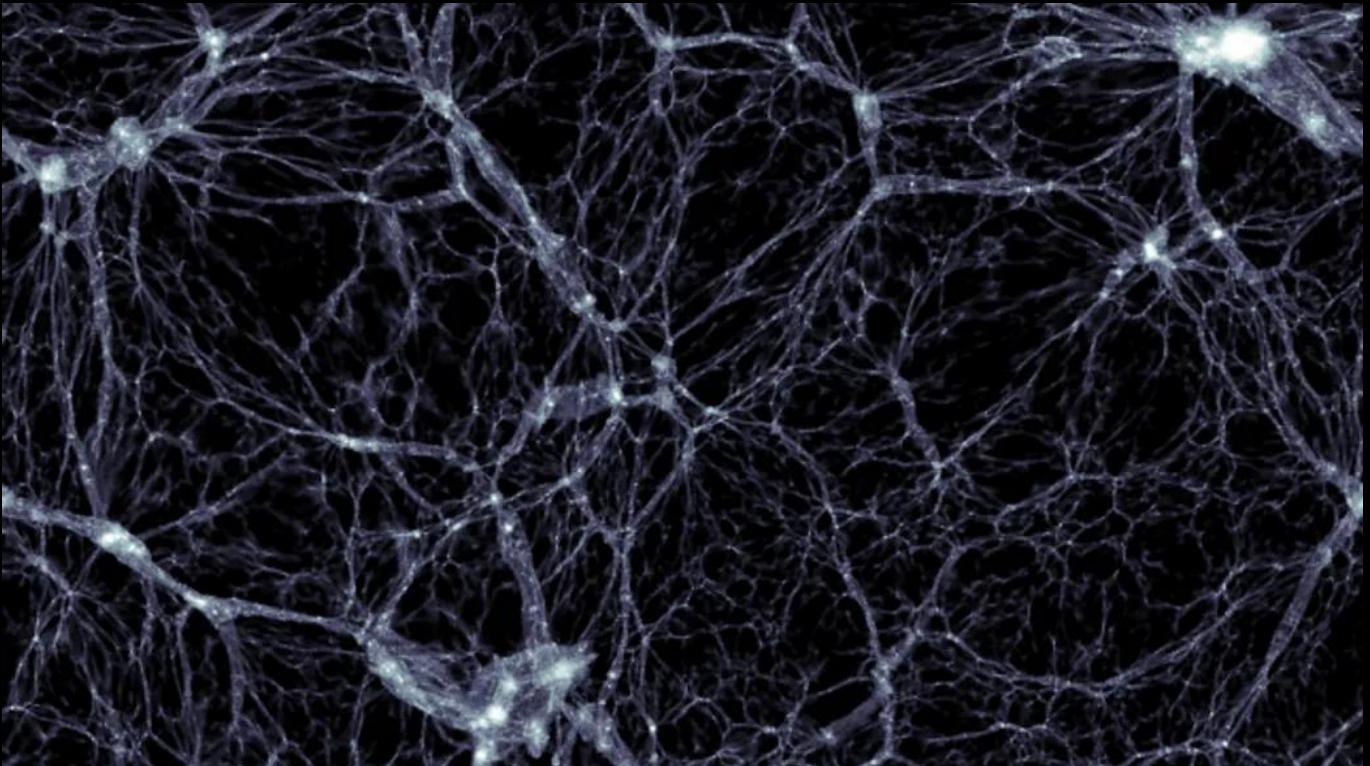
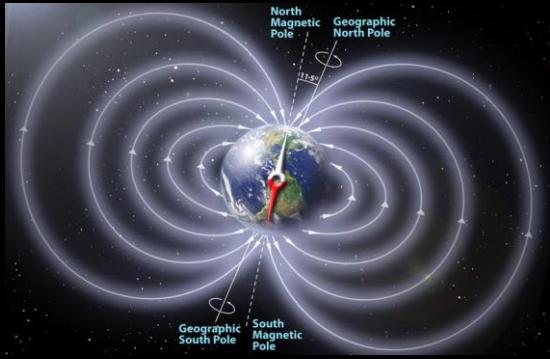


# Primordial magnetic fields and the matter power spectrum

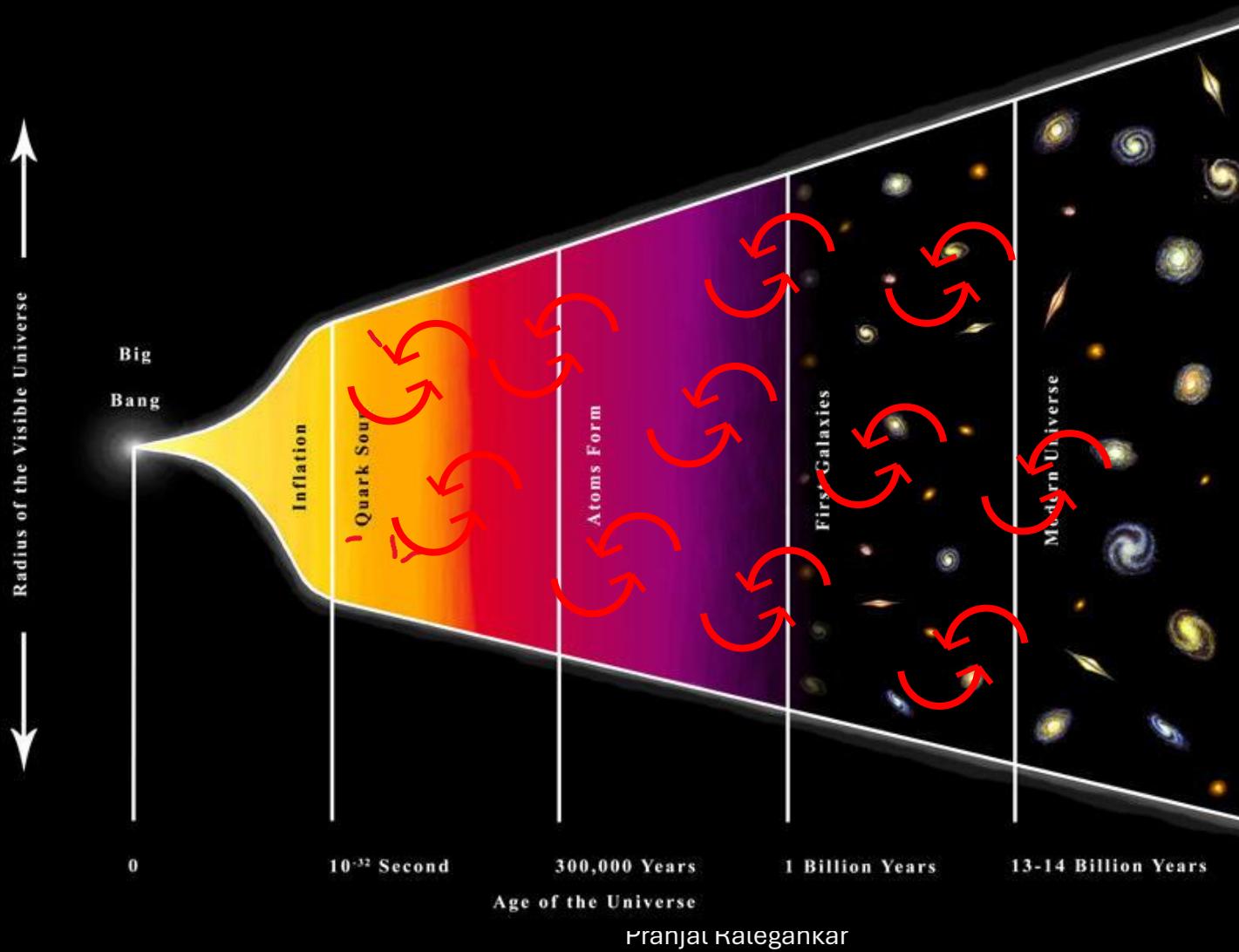
Pranjal Ralegankar  
Postdoctoral scientist, SISSA

Image source: Pauline Voß for Quanta Magazine

# Ubiquitous Magnetic Fields

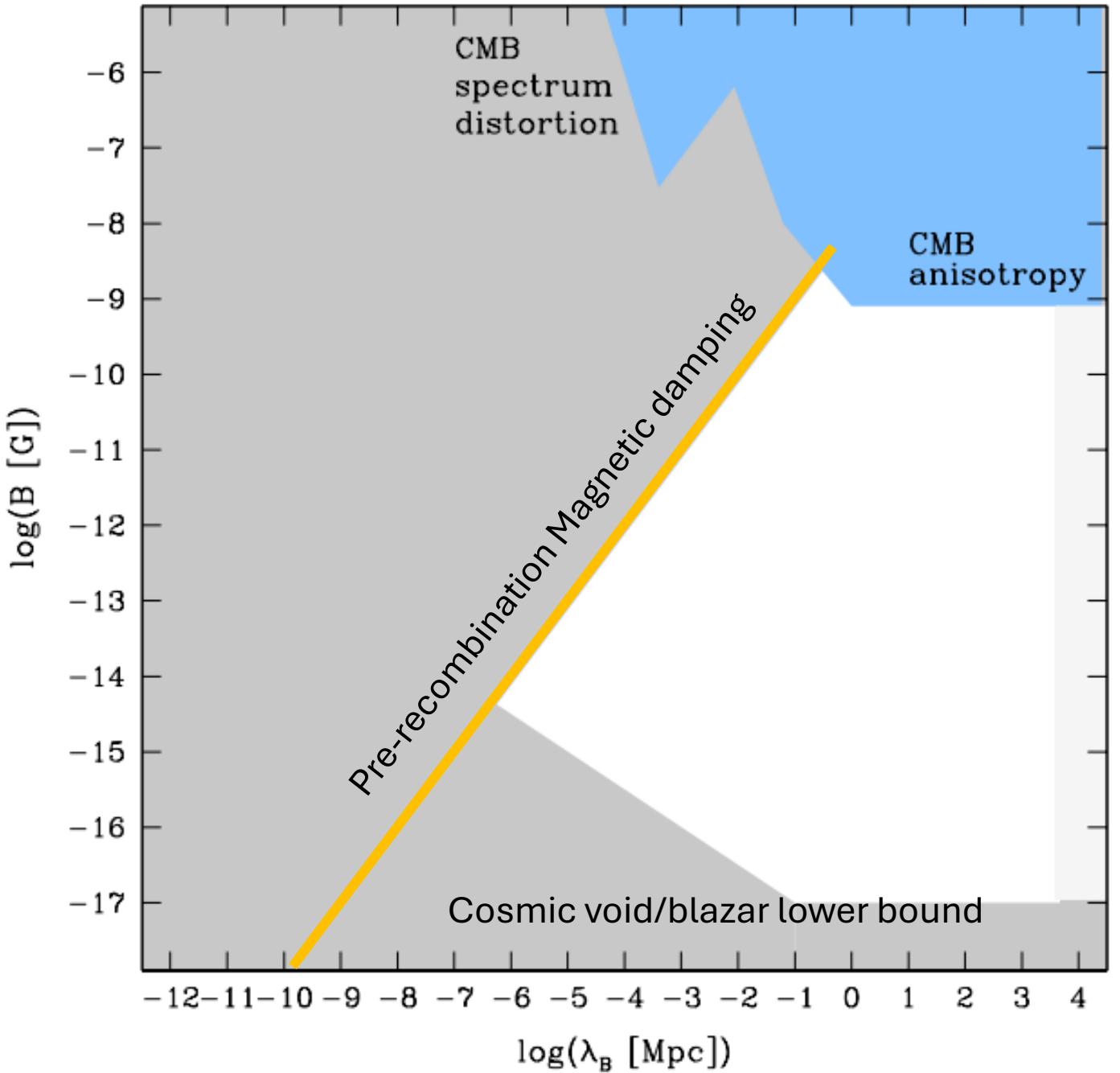


# Primordial: Produced by Big Bang plasma

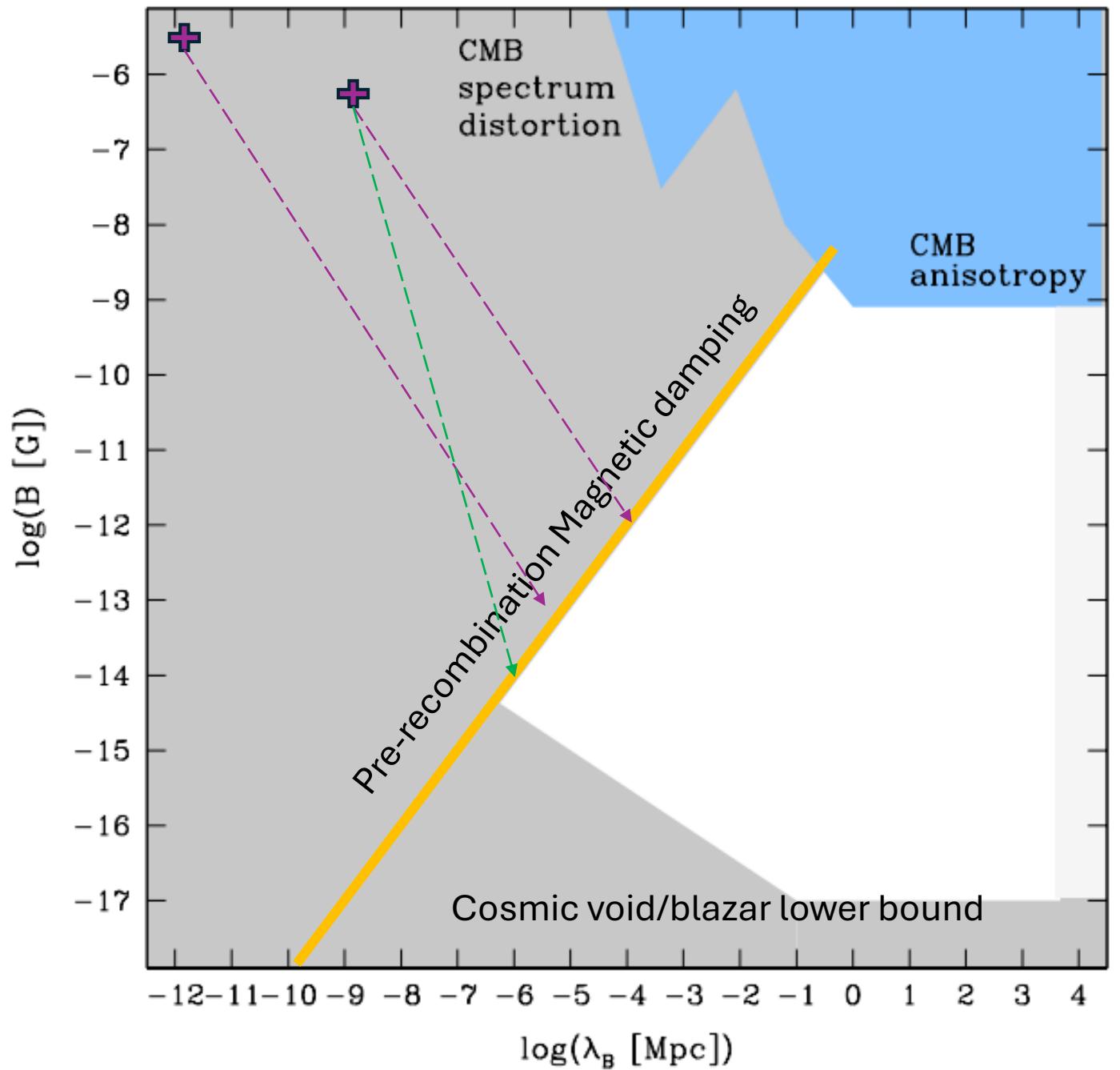


# Allowed PMF parameter space

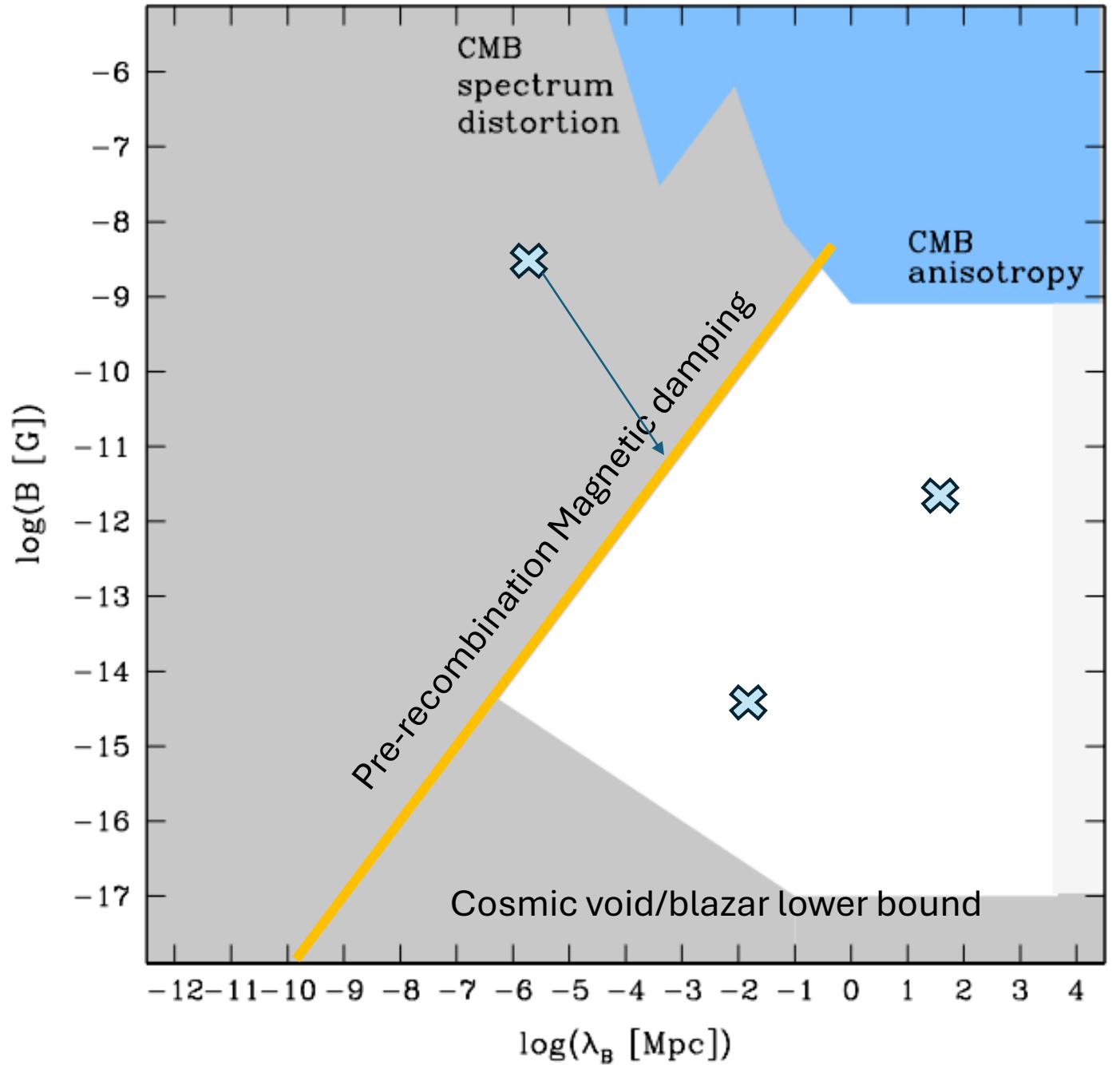
Durrer and Neronov 2013



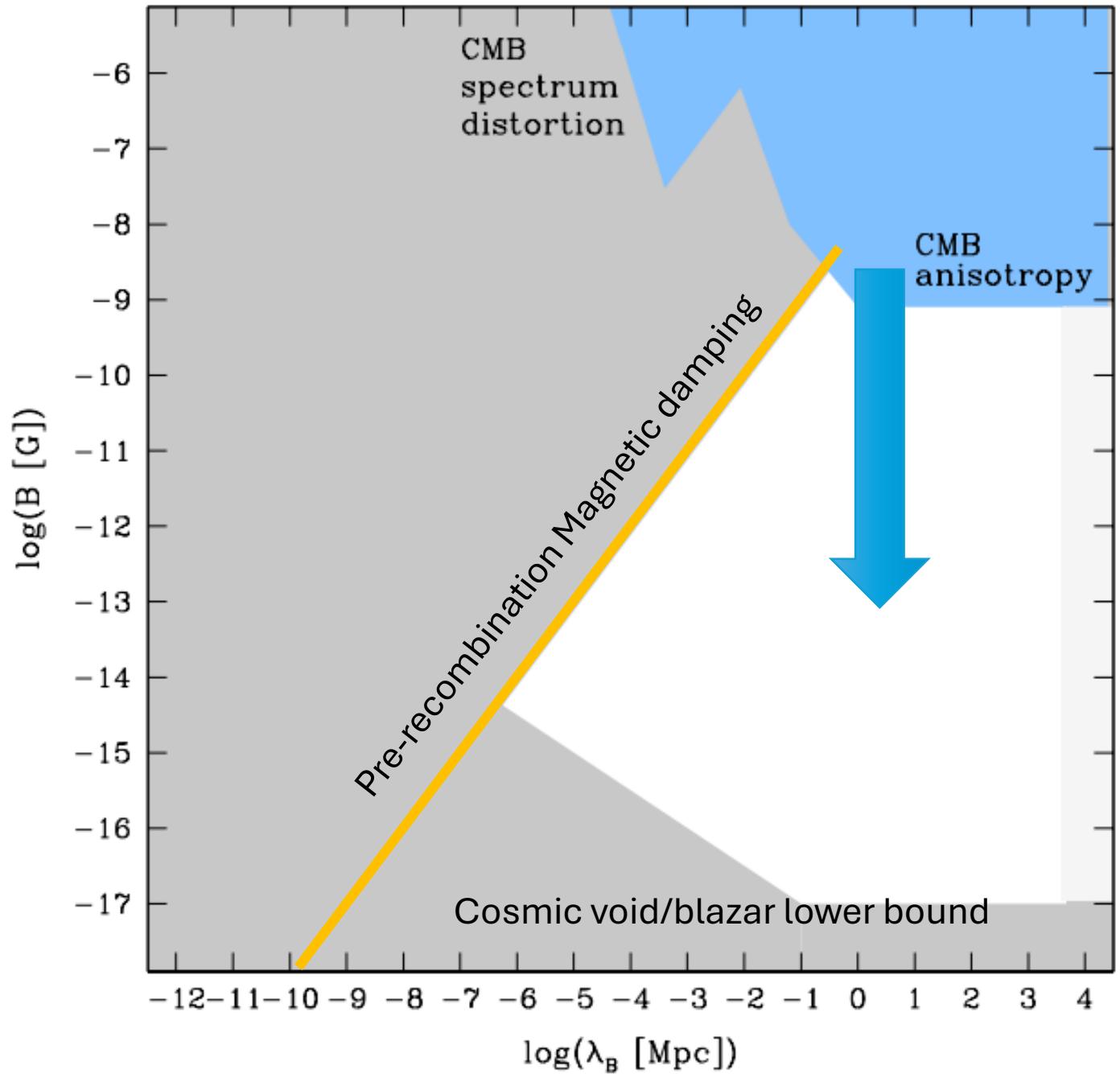
PMFs  
generated post  
inflation lie on  
the damping  
line



Inflation  
generated  
PMFs can be  
anywhere on  
the right of  
damping line

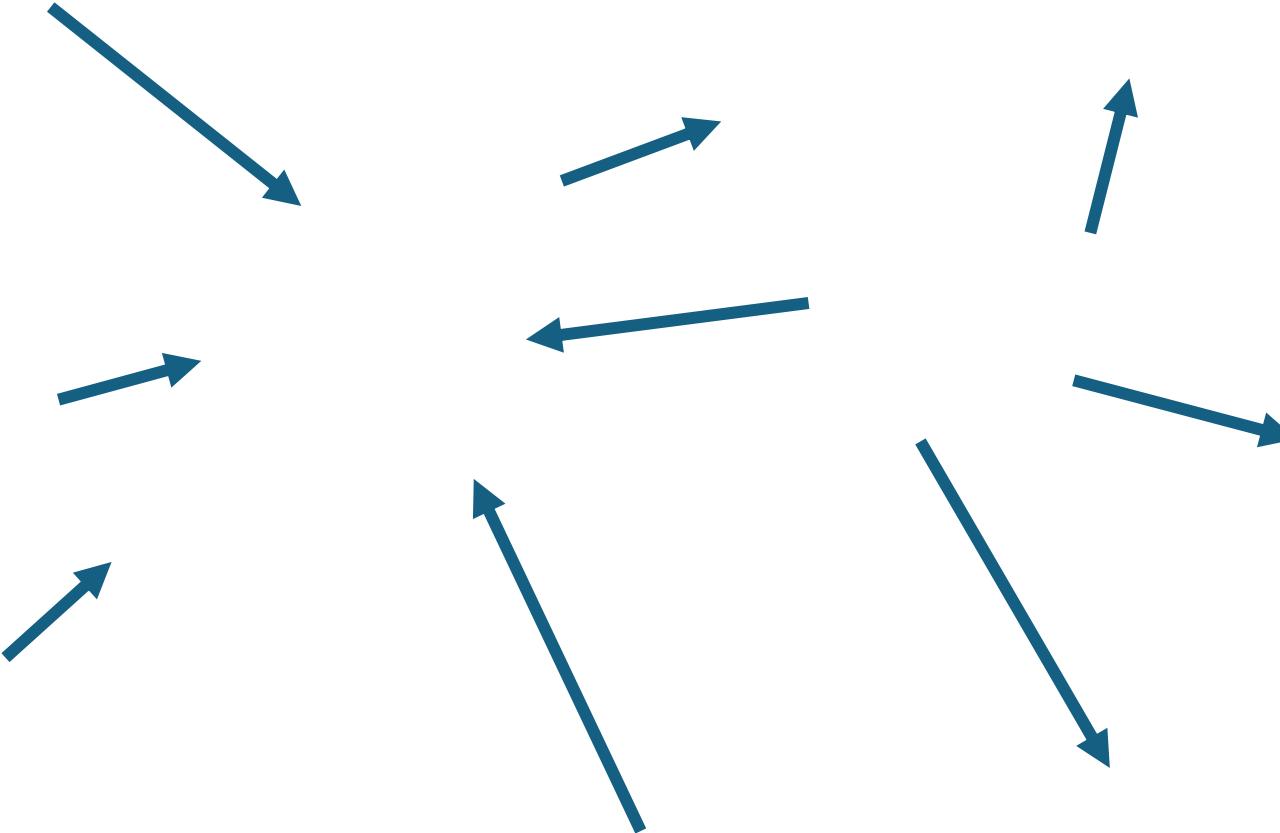


Goal: test the primordial hypothesis of magnetic fields

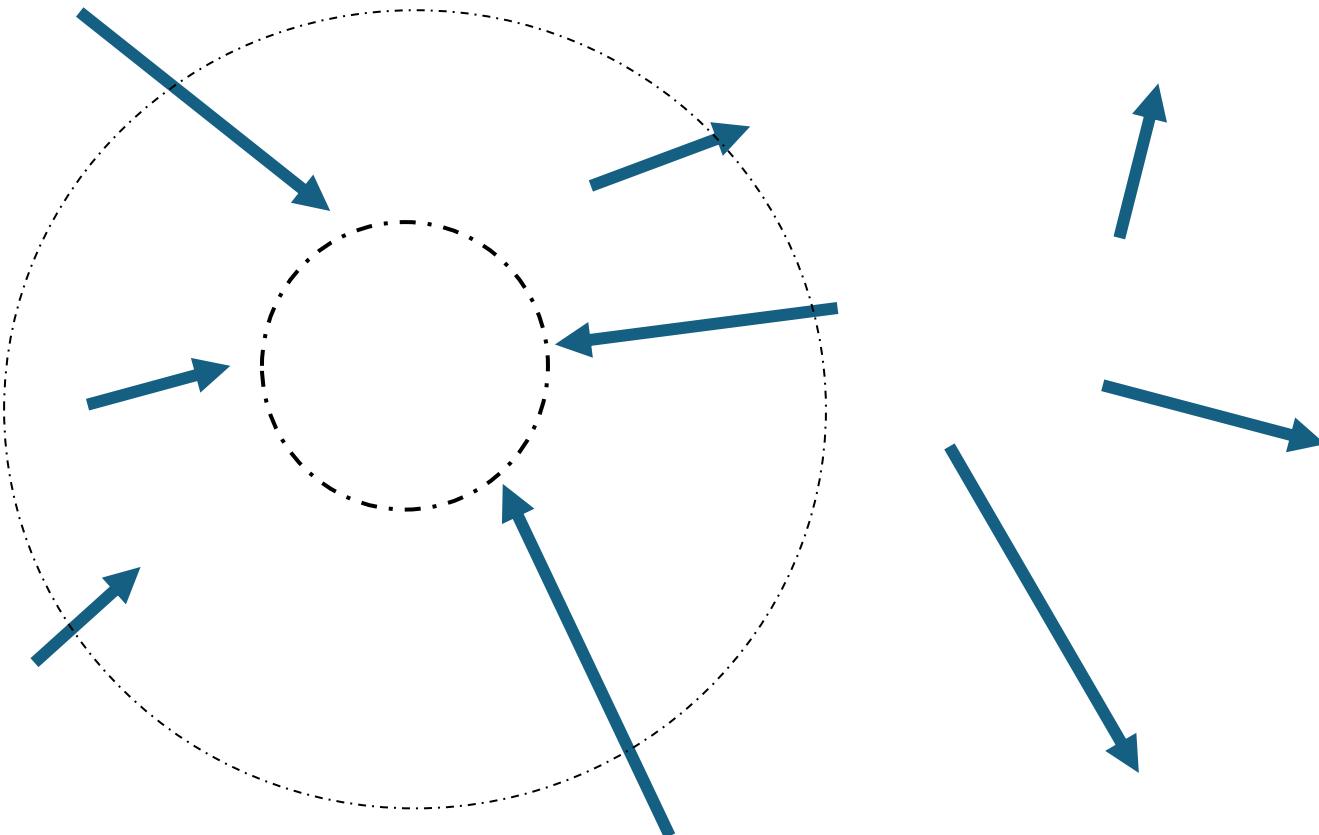


# Primordial Magnetic Fields enhance density perturbations

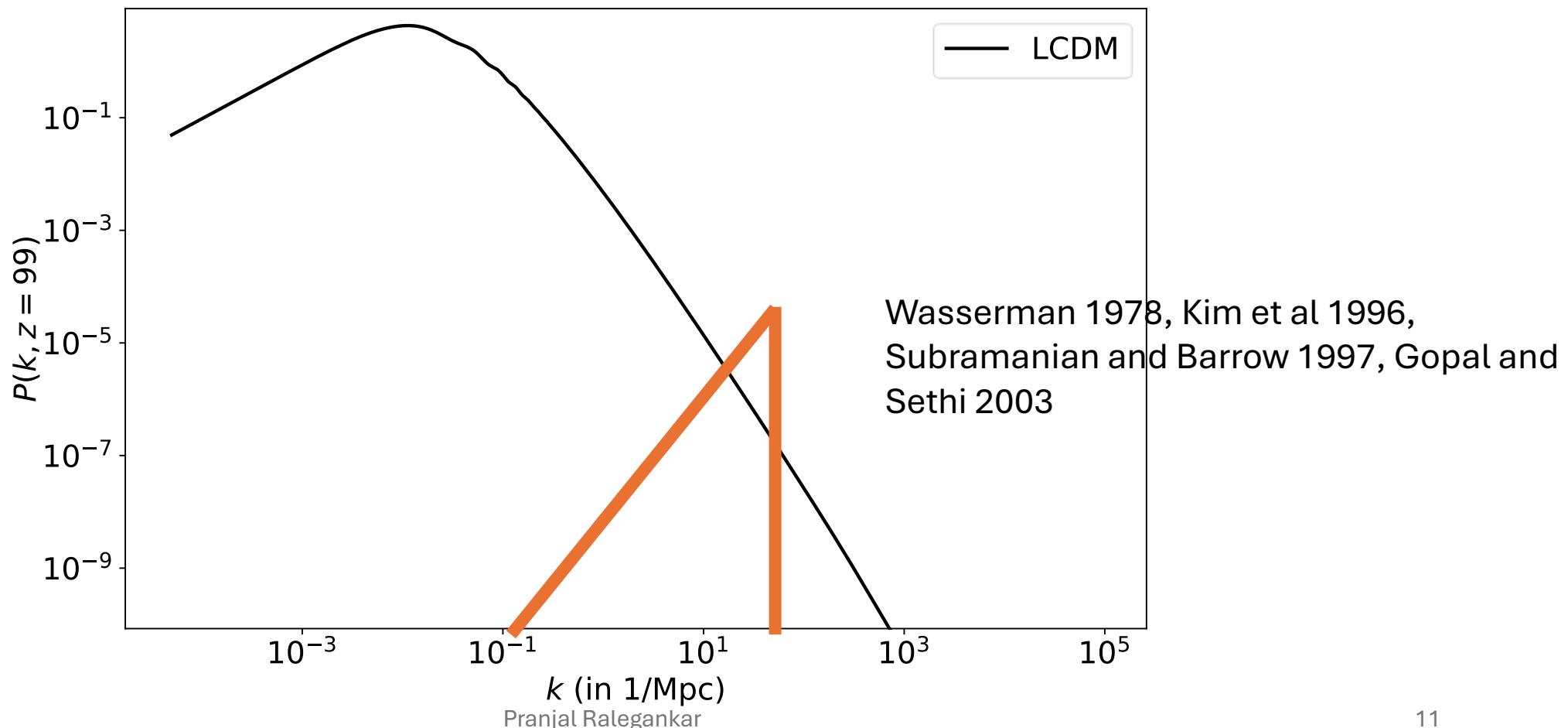
# Primordial Magnetic Fields enhance density perturbations



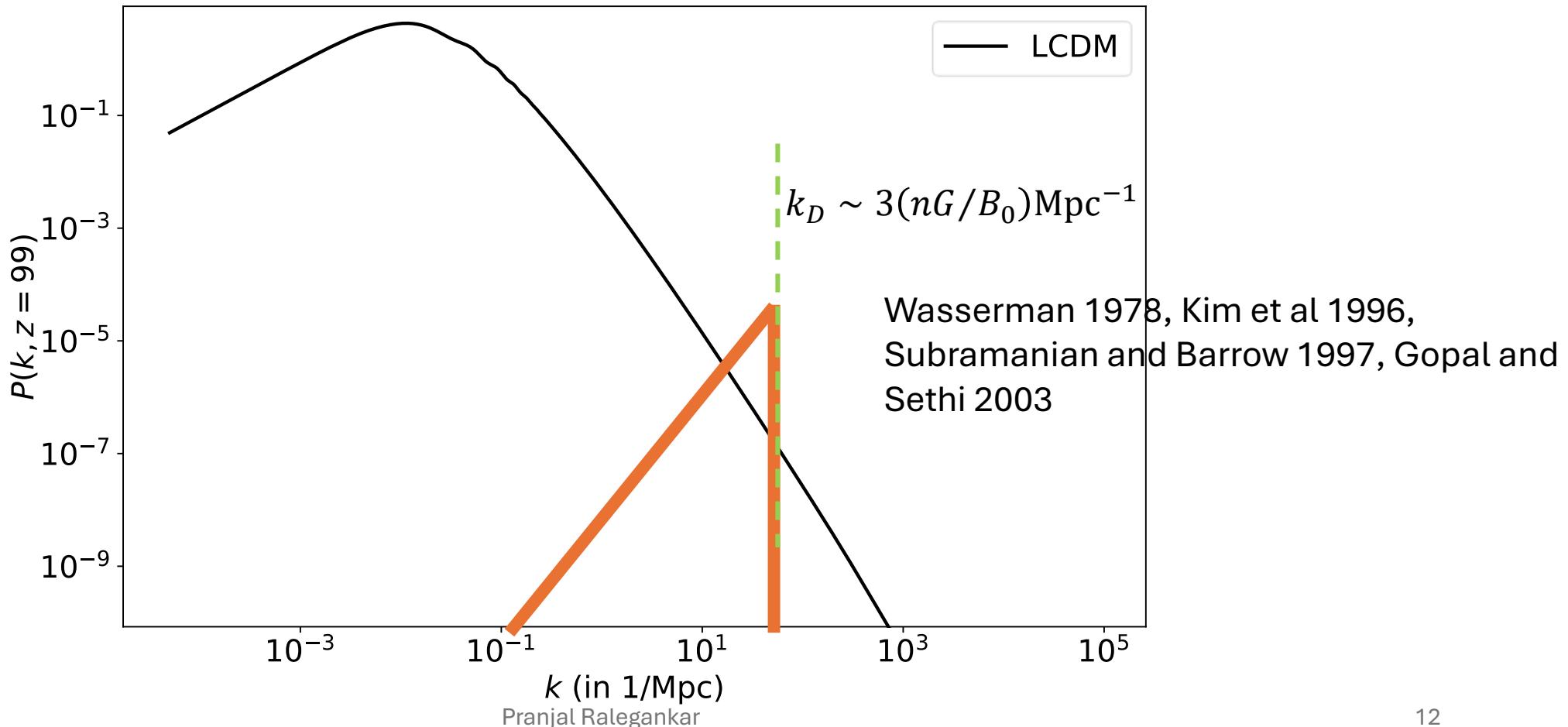
# Primordial Magnetic Fields enhance density perturbations



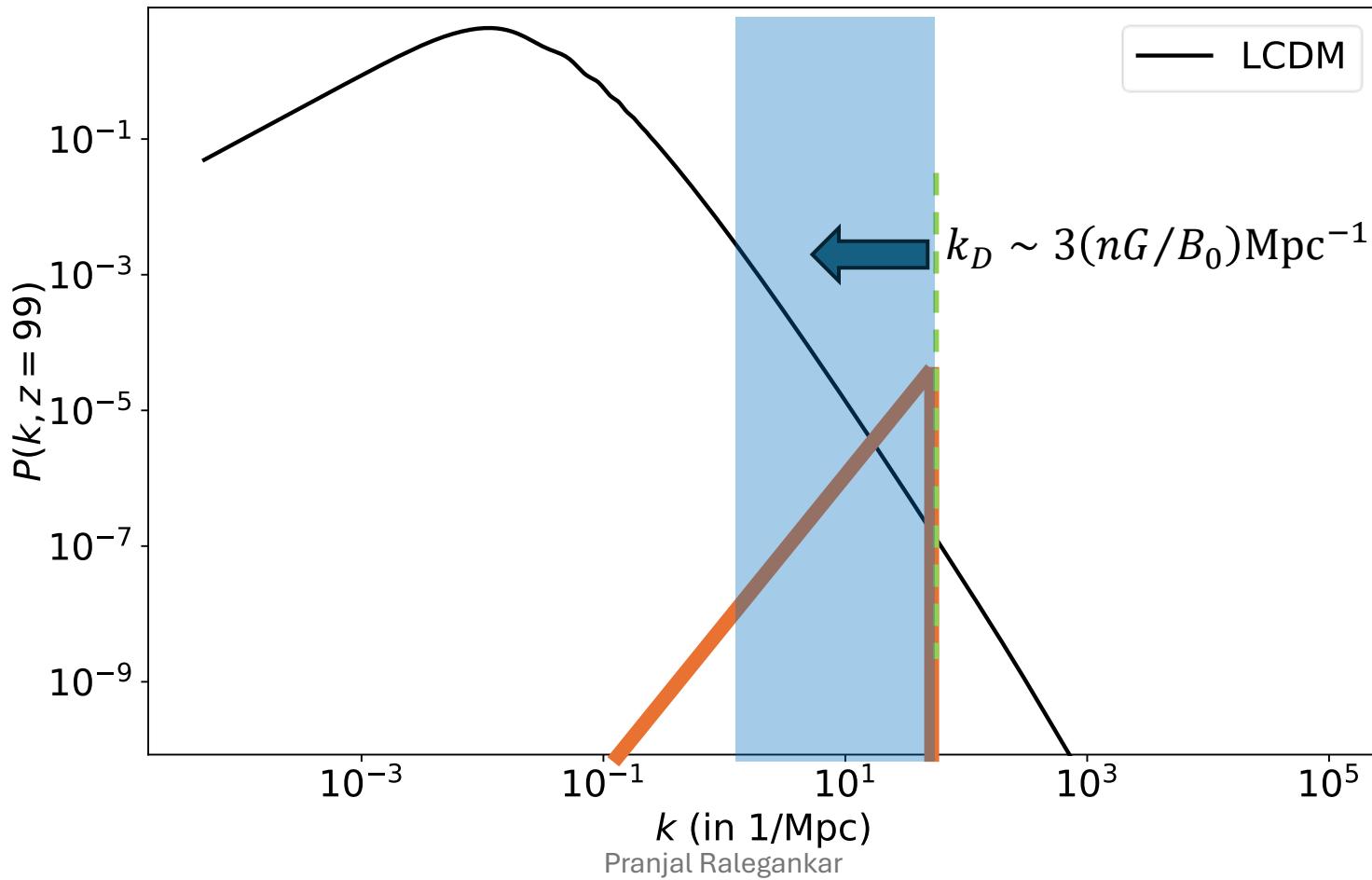
# Primordial Magnetic Fields enhance power spectrum on small scales



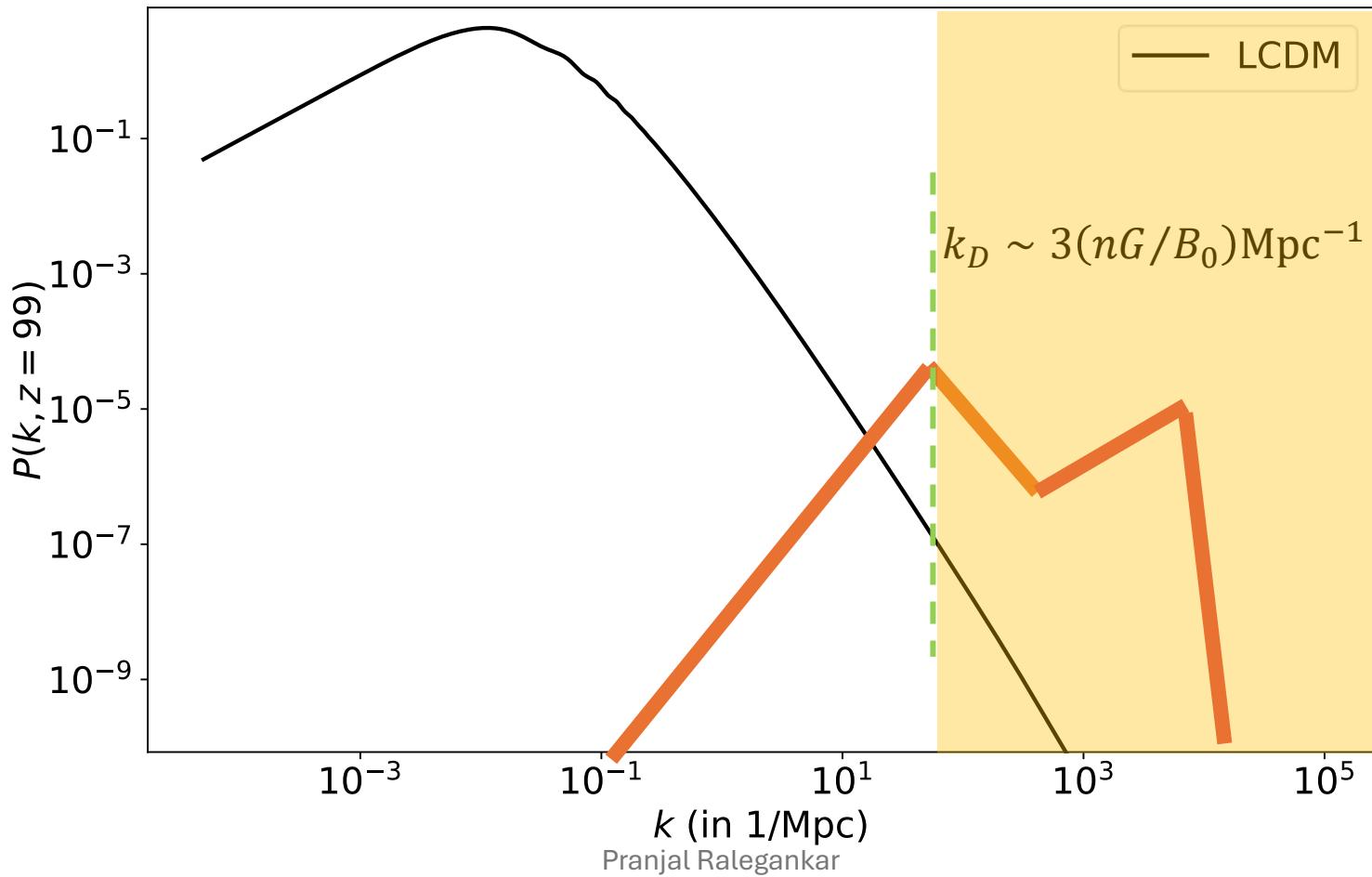
# Backreaction from baryons suppresses baryon density perturbations below Magnetic damping (Jeans) scale



# Part 1: Enhanced baryon fraction above jeans scale



# Part 2: Dark matter minihalos below jeans scale



# Part 1

Enhancing baryon fraction through Primordial  
magnetic fields

Arxiv: 2402.14079

# Post-recombination Ideal MHD

$$\frac{\partial (\vec{B})}{\partial t} = \frac{\nabla \times (\vec{v}_b \times \vec{B})}{a}$$

$$\frac{\partial \vec{v}_b}{\partial t} + H \vec{v}_b + \frac{(\vec{v}_b \cdot \nabla) \vec{v}_b}{a} = \frac{(\nabla \times \vec{B}) \times \vec{B}}{4\pi a^5 \rho_b} - \frac{c_b^2 \nabla \delta_b}{a} - \frac{\nabla \phi}{a}$$

$$\frac{\partial \delta_b}{\partial t} = -\frac{\nabla \cdot \vec{v}_b}{a} - \frac{\nabla \cdot (\delta_b \vec{v}_b)}{a}$$

$$\nabla^2 \phi = \frac{a^2}{2M_{Pl}^2} (\rho_b \delta_b + \rho_{DM} \delta_{DM})$$

$$\frac{\partial^2 \delta_{DM}}{\partial a^2} + \left[ \frac{\partial \ln(a^2 H)}{\partial \ln a} + 1 \right] \frac{\partial \delta_{DM}}{a \partial a} = \frac{\nabla^2 \phi}{(a^2 H)^2}$$

# Post-recombination Ideal MHD

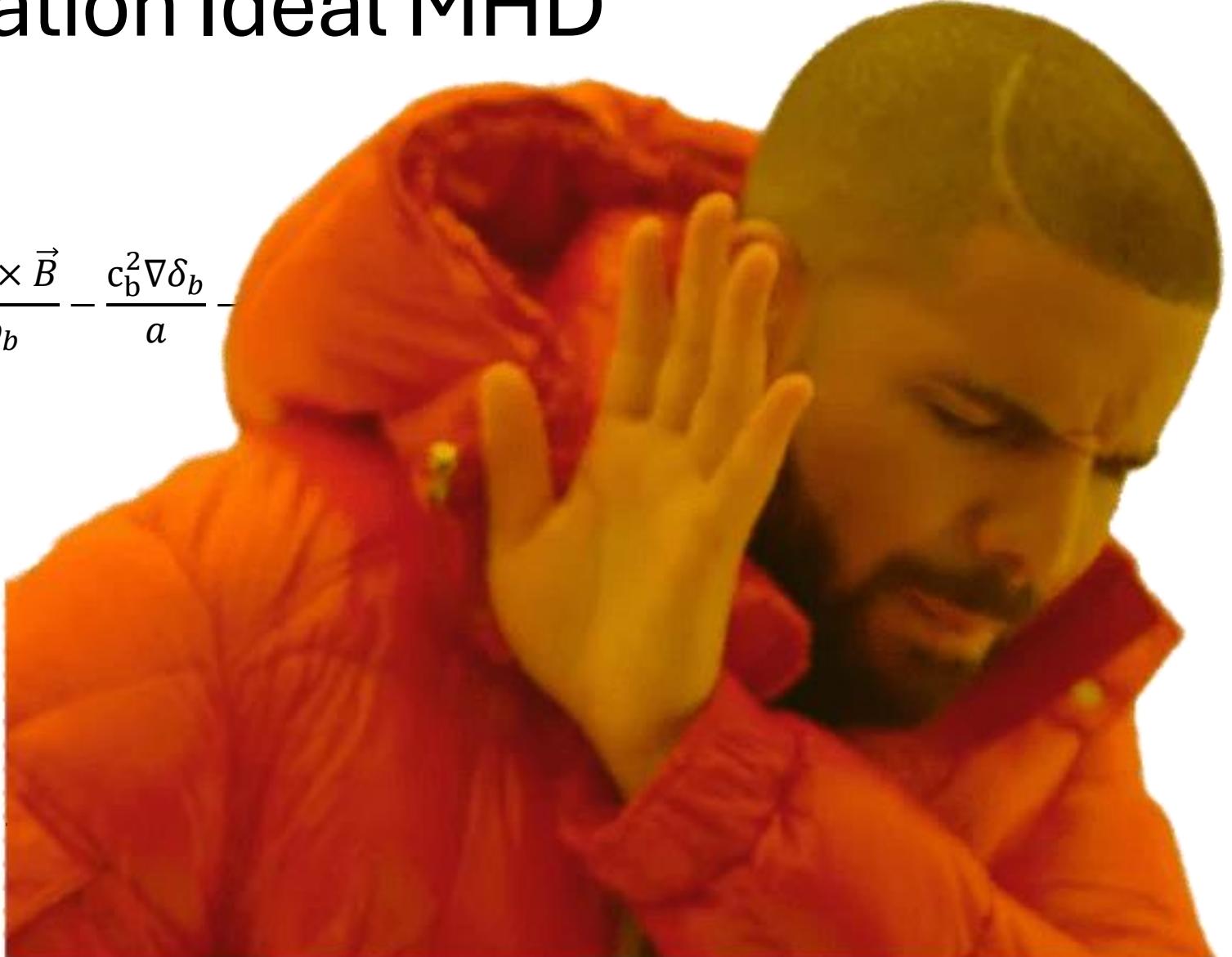
$$\frac{\partial (\vec{B})}{\partial t} = \frac{\nabla \times (\vec{v}_b \times \vec{B})}{a}$$

$$\frac{\partial \vec{v}_b}{\partial t} + H \vec{v}_b + \frac{(\vec{v}_b \cdot \nabla) \vec{v}_b}{a} = \frac{(\nabla \times \vec{B}) \times \vec{B}}{4\pi a^5 \rho_b} - \frac{c_b^2 \nabla \delta_b}{a} -$$

$$\frac{\partial \delta_b}{\partial t} = -\frac{\nabla \cdot \vec{v}_b}{a} - \frac{\nabla \cdot (\delta_b \vec{v}_b)}{a}$$

$$\nabla^2 \phi = \frac{a^2}{2M_{Pl}^2} (\rho_b \delta_b + \rho_{DM} \delta_{DM})$$

$$\frac{\partial^2 \delta_{DM}}{\partial a^2} + \left[ \frac{\partial \ln(a^2 H)}{\partial \ln a} + 1 \right] \frac{\partial \delta_{DM}}{\partial a} =$$



# Post-recombination Ideal MHD

$$\frac{\partial (a^2 \vec{B})}{\partial t} = \frac{\nabla \times (\vec{v}_b \times a^2 \vec{B})}{a}$$

$$\frac{\partial \vec{v}_b}{\partial t} + H \vec{v}_b + \frac{(\vec{v}_b \cdot \nabla) \vec{B}}{a} = - \frac{\vec{B}}{a} - \frac{c_b^2 \nabla \delta_b}{a} - \frac{\nabla \phi}{a}$$

$$\frac{\partial \delta_b}{\partial t} = - \frac{\nabla \cdot \vec{v}_b}{a}$$

$$\nabla^2$$

Focus on large scales, linear limit  
 $\delta \ll 1, v_b \ll aH$

# Post-recombination Ideal MHD linear limit

$$\frac{\partial (\vec{B})}{\partial t} = 0$$

$$\frac{\partial^2 \delta_b}{\partial a^2} + \frac{3}{2} \frac{\partial \delta_b}{a \partial a} = - \frac{\nabla \cdot (\nabla \times \vec{B}) \times \vec{B}}{(4\pi a^3 \rho_b) a^5 H^2} + \frac{\nabla^2 \phi}{(a^2 H)^2}$$

$$\nabla^2 \phi = \frac{a^2}{2M_{Pl}^2} (\rho_b \delta_b + \rho_{DM} \delta_{DM})$$

$$\frac{\partial^2 \delta_{DM}}{\partial a^2} + \frac{3}{2} \frac{\partial \delta_{DM}}{a \partial a} = \frac{\nabla^2 \phi}{(a^2 H)^2}$$

# Comoving Magnetic fields are frozen

$$\frac{\partial (\vec{B})}{\partial t} = 0$$

$$\frac{\partial^2 \delta_b}{\partial a^2} + \frac{3}{2} \frac{\partial \delta_b}{a \partial a} = - \frac{\nabla \cdot (\nabla \times \vec{B}) \times \vec{B}}{(4\pi a^3 \rho_b) a^5 H^2} + \frac{\nabla^2 \phi}{(a^2 H)^2}$$

$$\nabla^2 \phi = \frac{a^2}{2M_{Pl}^2} (\rho_b \delta_b + \rho_{DM} \delta_{DM})$$

$$\frac{\partial^2 \delta_{DM}}{\partial a^2} + \frac{3}{2} \frac{\partial \delta_{DM}}{a \partial a} = \frac{\nabla^2 \phi}{(a^2 H)^2}$$

# Baryons driven by Lorentz force and gravity

$$\frac{\partial (\vec{B})}{\partial t} = 0$$

$$\frac{\partial^2 \delta_b}{\partial a^2} + \frac{3}{2} \frac{\partial \delta_b}{a \partial a} = - \frac{\nabla \cdot (\nabla \times \vec{B}) \times \vec{B}}{(4\pi a^3 \rho_b) a^5 H^2} + \frac{\nabla^2 \phi}{(a^2 H)^2}$$

$$\nabla^2 \phi = \frac{a^2}{2M_{Pl}^2} (\rho_b \delta_b + \rho_{DM} \delta_{DM})$$

$$\frac{\partial^2 \delta_{DM}}{\partial a^2} + \frac{3}{2} \frac{\partial \delta_{DM}}{a \partial a} = \frac{\nabla^2 \phi}{(a^2 H)^2}$$

# Dark matter only influenced by gravity

$$\frac{\partial (\vec{B})}{\partial t} = 0$$

$$\frac{\partial^2 \delta_b}{\partial a^2} + \frac{3}{2} \frac{\partial \delta_b}{a \partial a} = - \frac{\nabla \cdot (\nabla \times \vec{B}) \times \vec{B}}{(4\pi a^3 \rho_b) a^5 H^2} + \frac{\nabla^2 \phi}{(a^2 H)^2}$$

$$\nabla^2 \phi = \frac{a^2}{2M_{Pl}^2} (\rho_b \delta_b + \rho_{DM} \delta_{DM})$$

$$\frac{\partial^2 \delta_{DM}}{\partial a^2} + \frac{3}{2} \frac{\partial \delta_{DM}}{a \partial a} = \frac{\nabla^2 \phi}{(a^2 H)^2}$$

# Star of the show: $S_0$ term

$$\frac{\partial (\vec{B})}{\partial t} = 0$$

$$\frac{\partial^2 \delta_b}{\partial a^2} + \frac{3}{2} \frac{\partial \delta_b}{a \partial a} = - \frac{\nabla \cdot (\nabla \times \vec{B}) \times \vec{B}}{(4\pi a^3 \rho_b) a^5 H^2} + \frac{\nabla^2 \phi}{(a^2 H)^2}$$

$$\nabla^2 \phi = \frac{a^2}{2M_{Pl}^2} (\rho_b \delta_b + \rho_{DM} \delta_{DM})$$

$$\frac{\partial^2 \delta_{DM}}{\partial a^2} + \frac{3}{2} \frac{\partial \delta_{DM}}{a \partial a} = \frac{\nabla^2 \phi}{(a^2 H)^2}$$

# Star of the show: $S_0$ term

$$\frac{\partial (\vec{B})}{\partial t} = 0$$

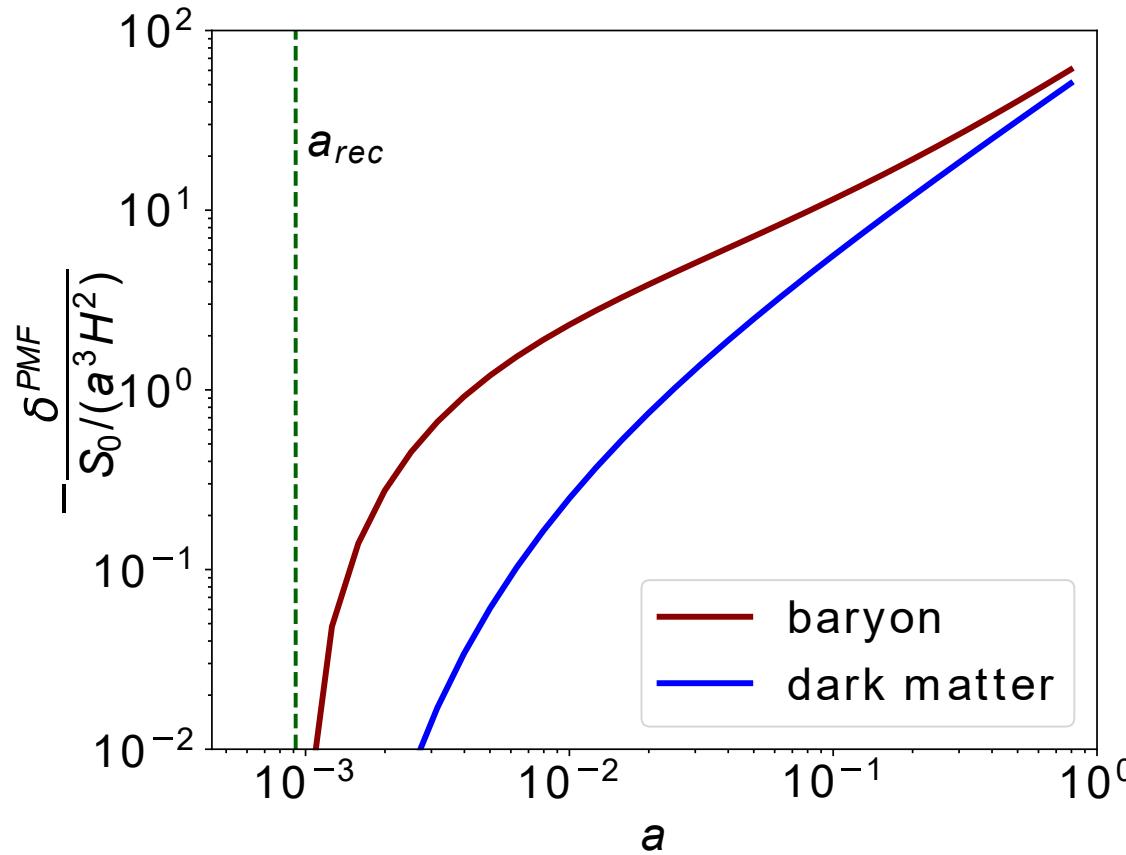
$$\frac{\partial^2 \delta_b}{\partial a^2} + \frac{3}{2} \frac{\partial \delta_b}{a \partial a} = -\frac{S_0}{a^2(a^3 H^2)} + \frac{\nabla^2 \phi}{(a^2 H)^2}$$

$$\nabla^2 \phi = \frac{a^2}{2M_{Pl}^2} (\rho_b \delta_b + \rho_{DM} \delta_{DM})$$

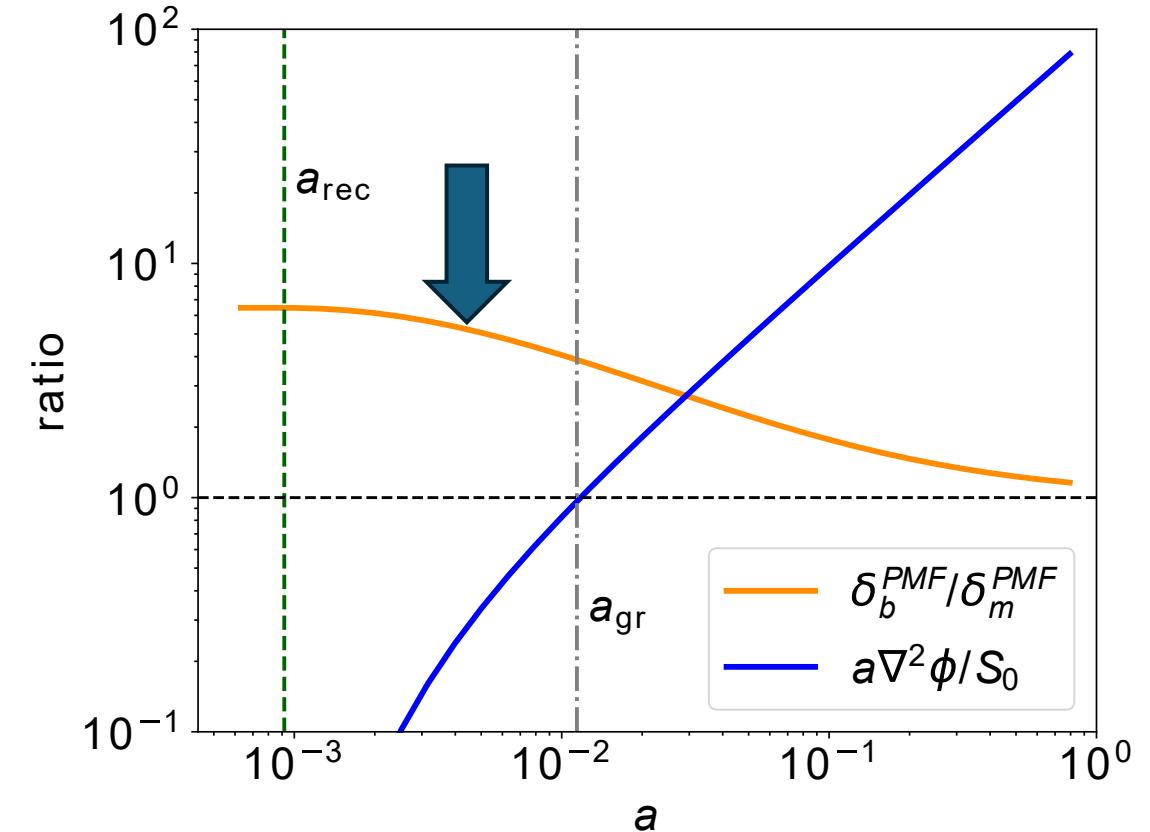
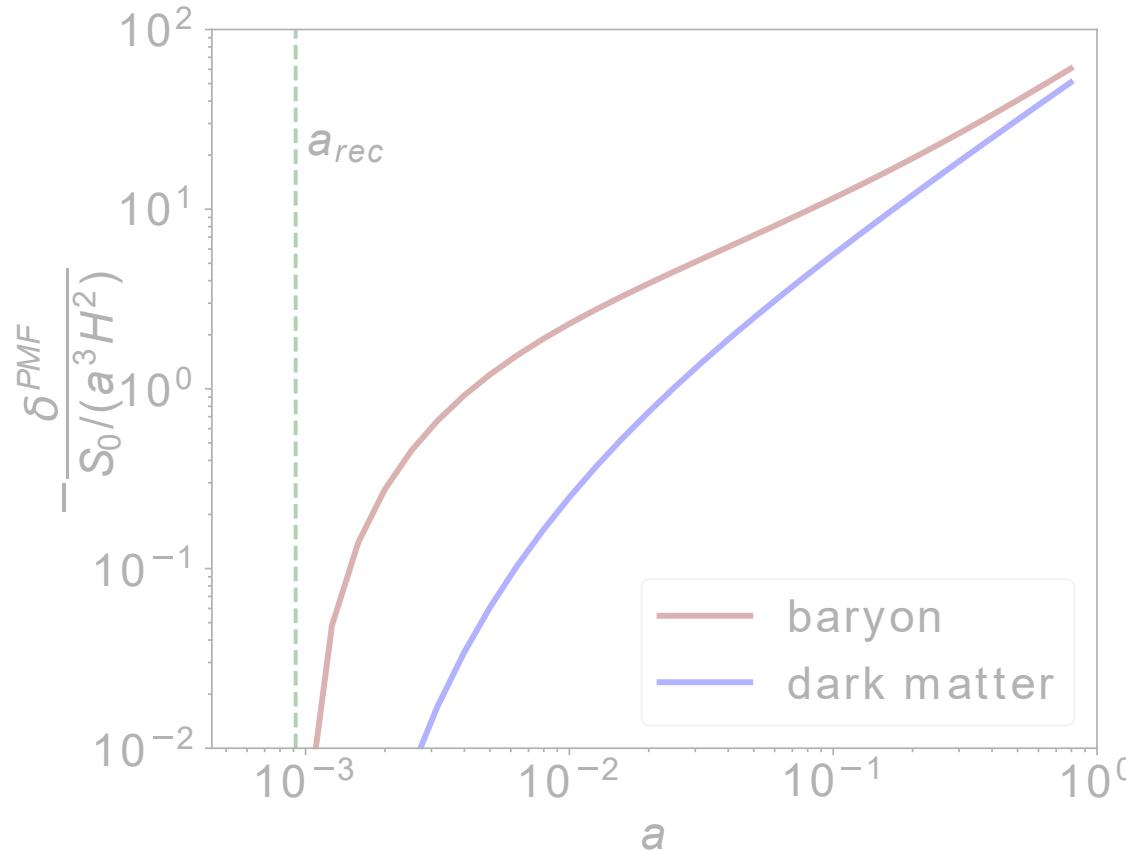
$$\frac{\partial^2 \delta_{DM}}{\partial a^2} + \frac{3}{2} \frac{\partial \delta_{DM}}{a \partial a} = \frac{\nabla^2 \phi}{(a^2 H)^2}$$

$$\frac{S_0}{a^3 H^2} = \frac{\nabla \cdot (\nabla \times \vec{B}) \times \vec{B}}{4\pi a^3 \rho_b (a^3 H^2)} = \text{constant}$$

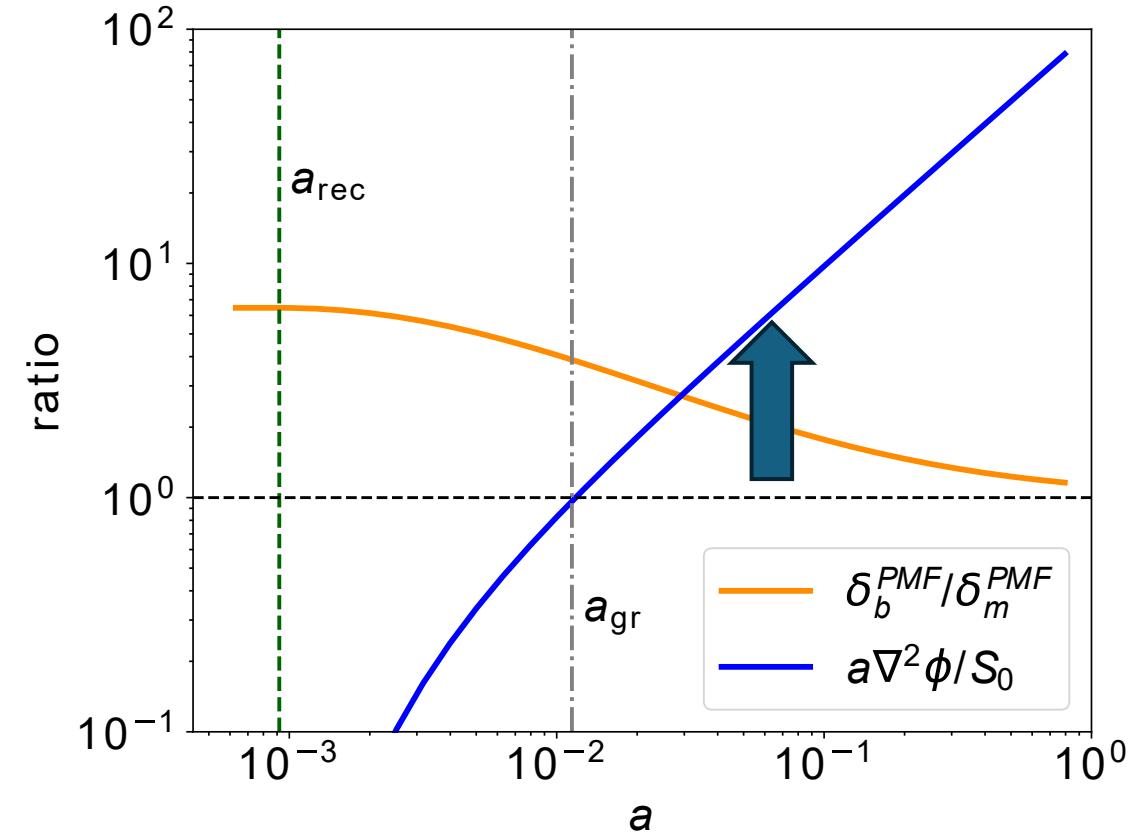
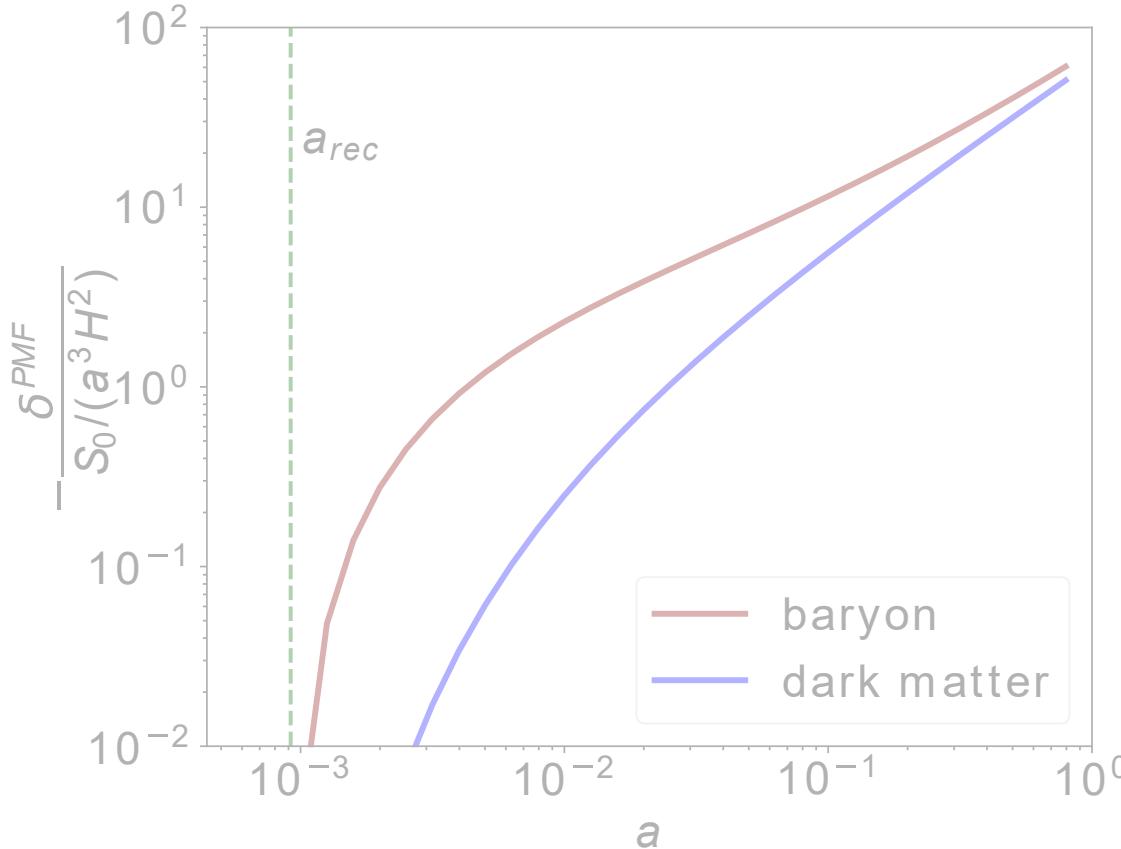
# $S_0$ sources baryon perturbations



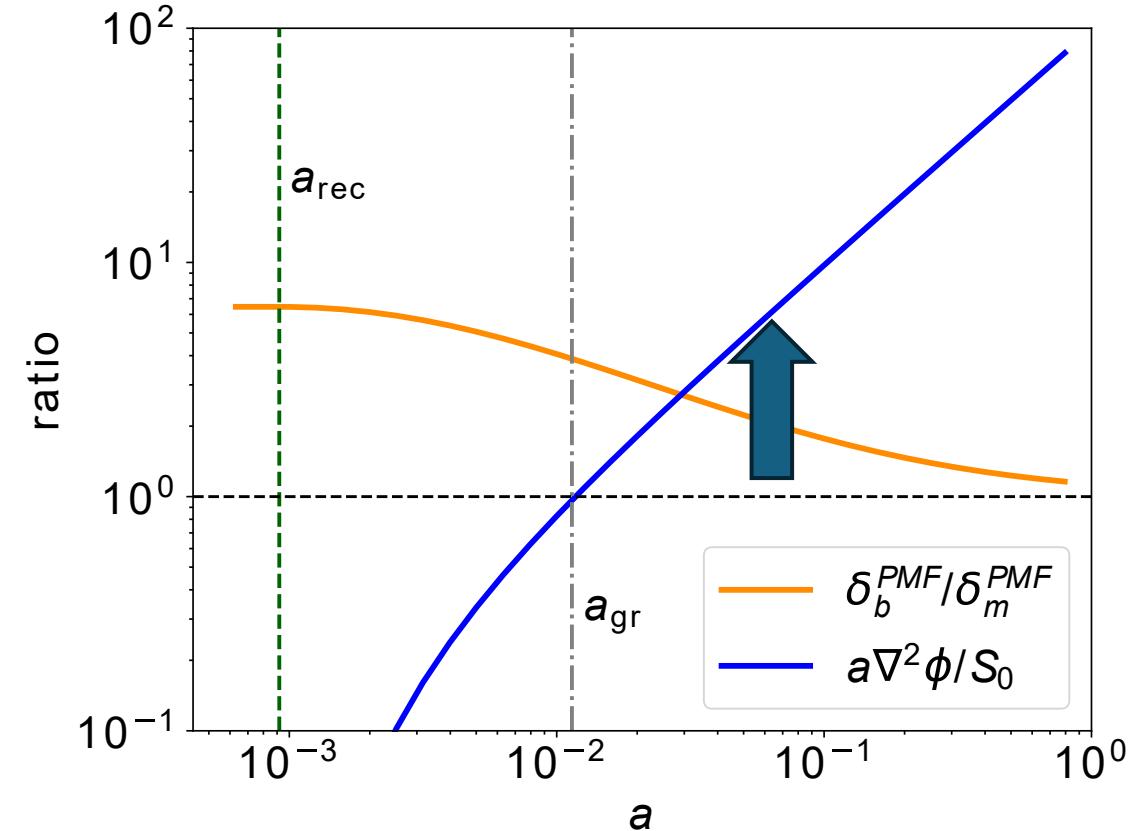
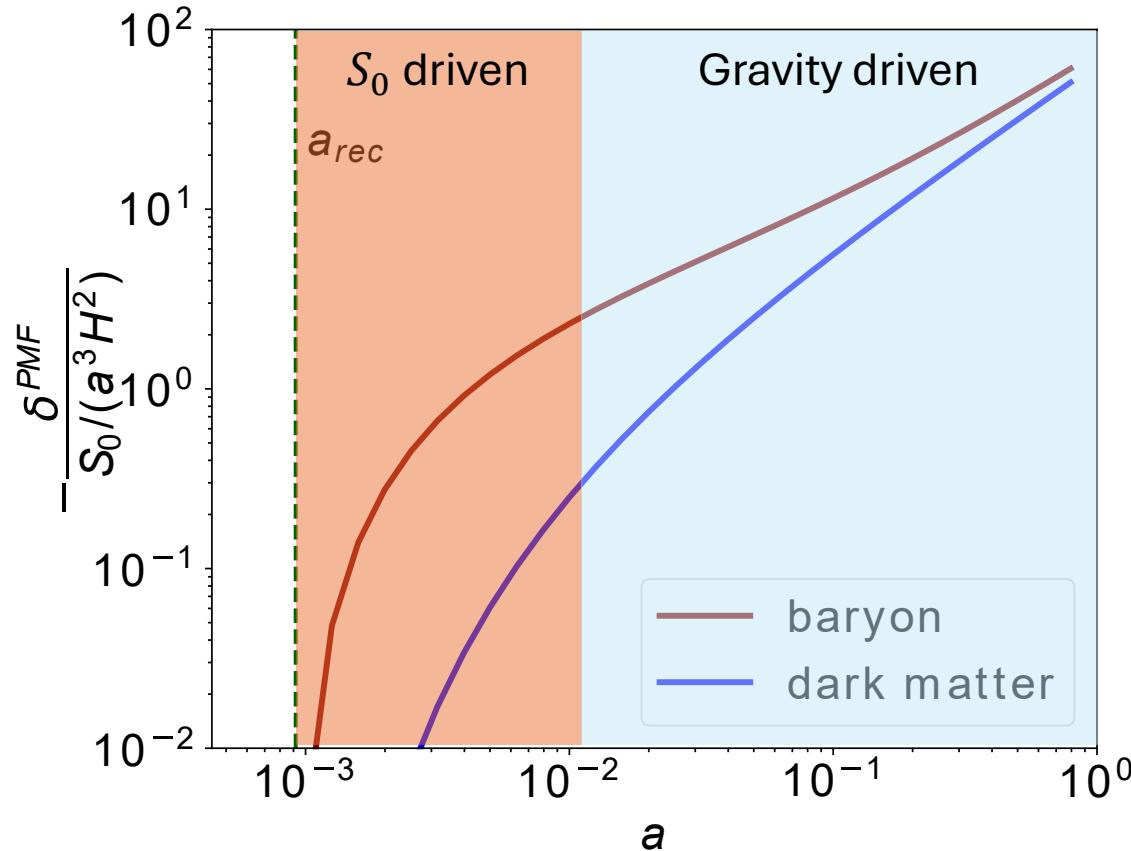
# Baryon fraction decreases with time



# Gravity quickly overcomes Lorentz force

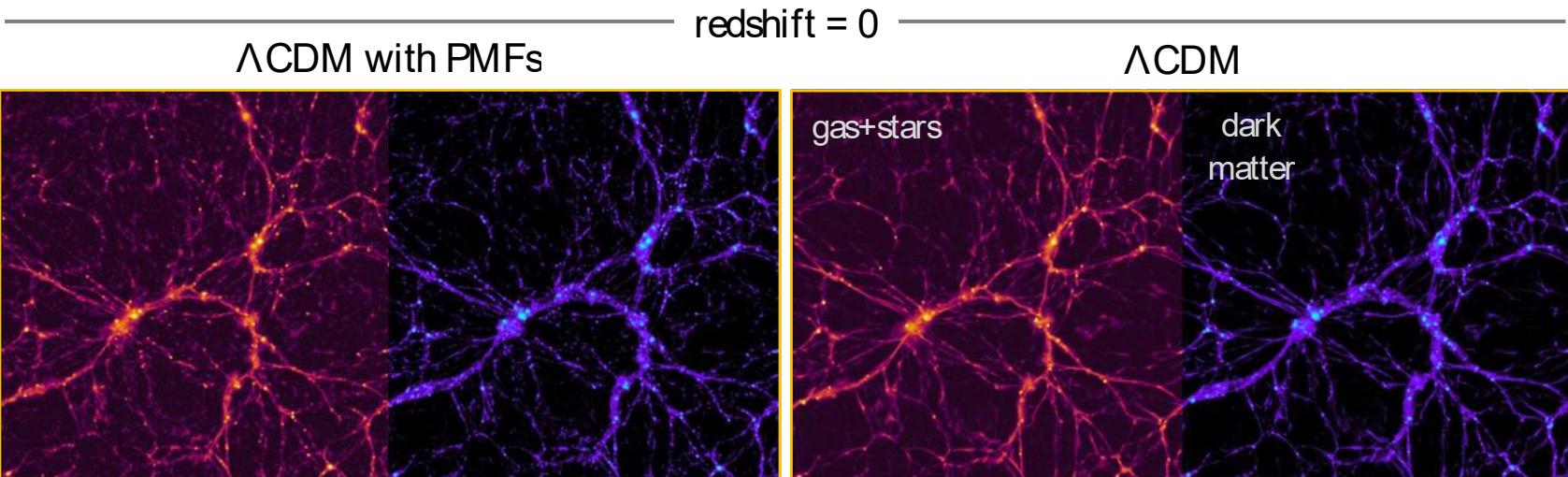
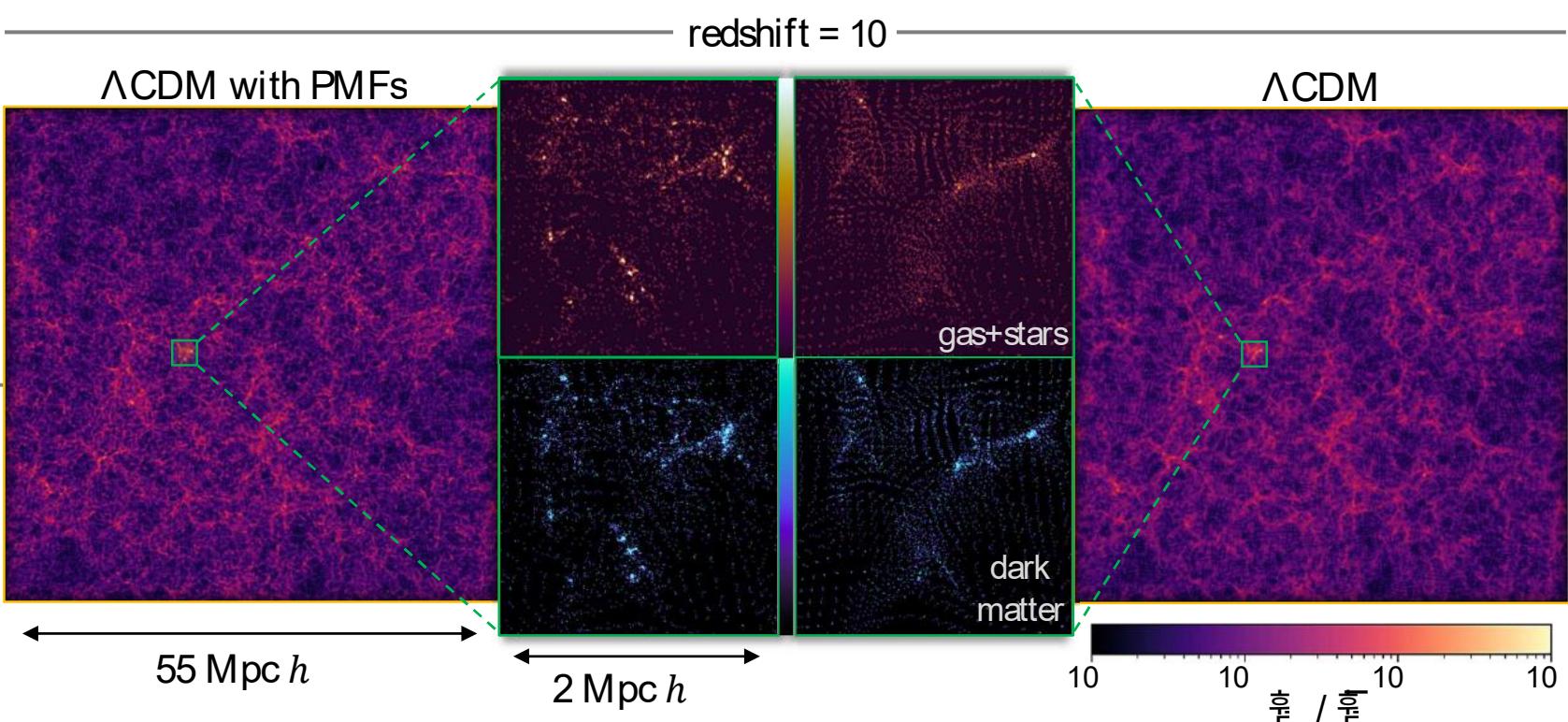
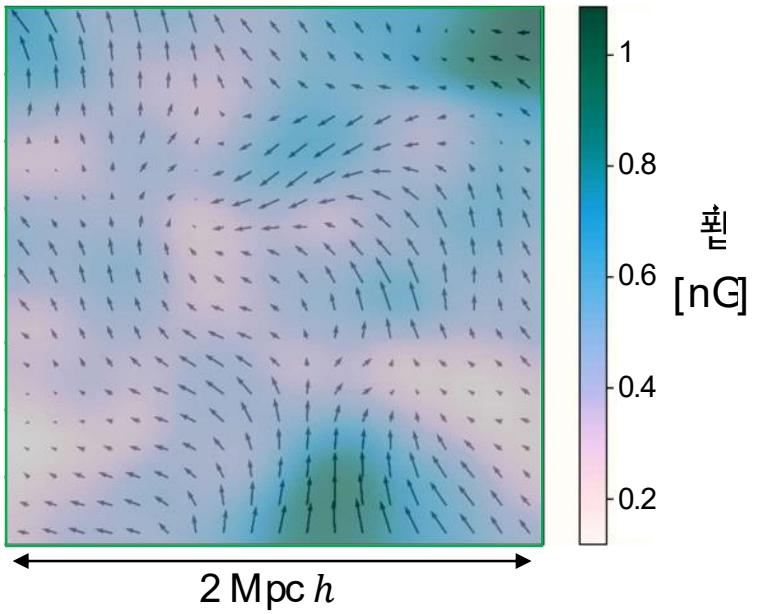


# Gravity quickly overcomes Lorentz force

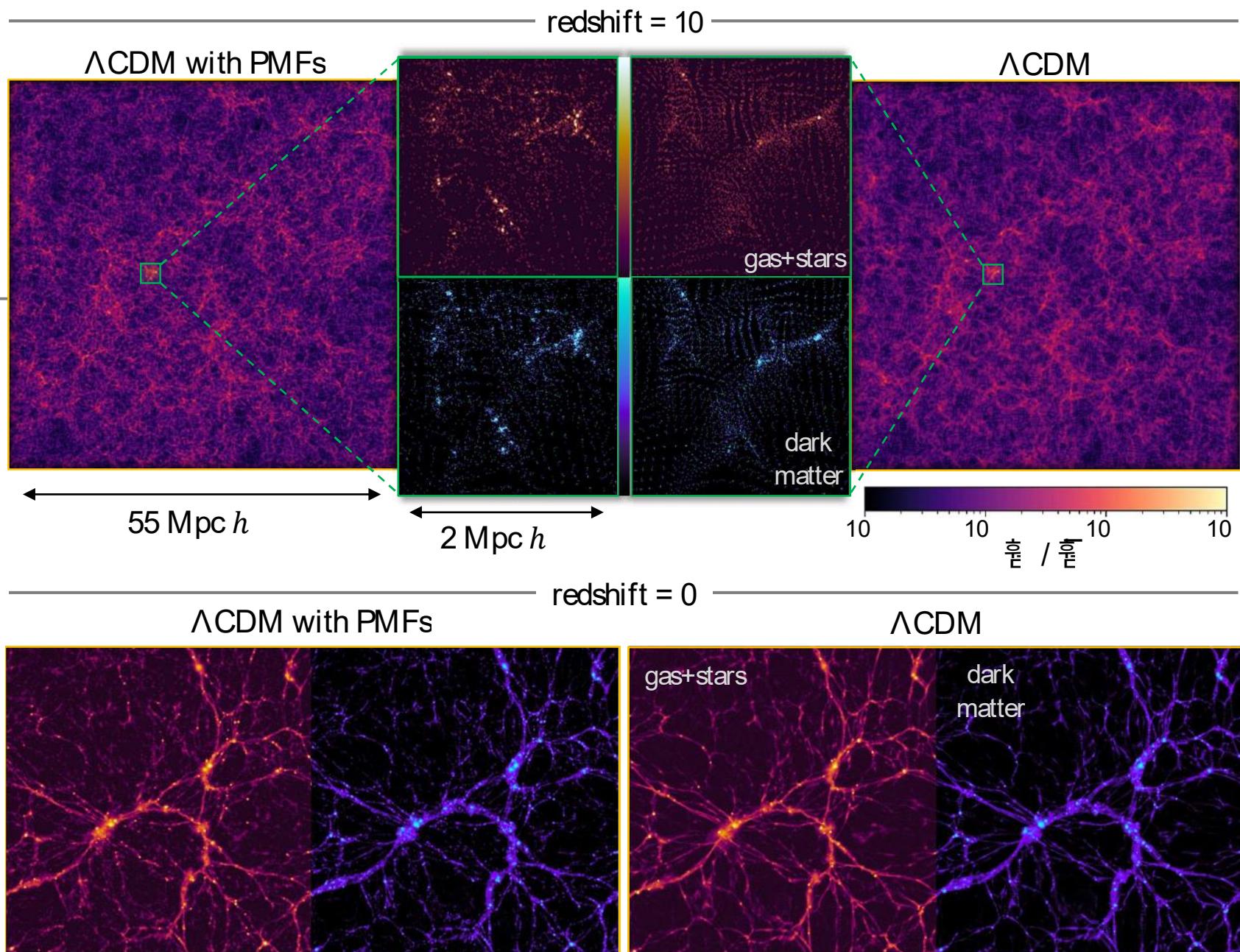


# Simulations

– Initial conditions: redshift = 99

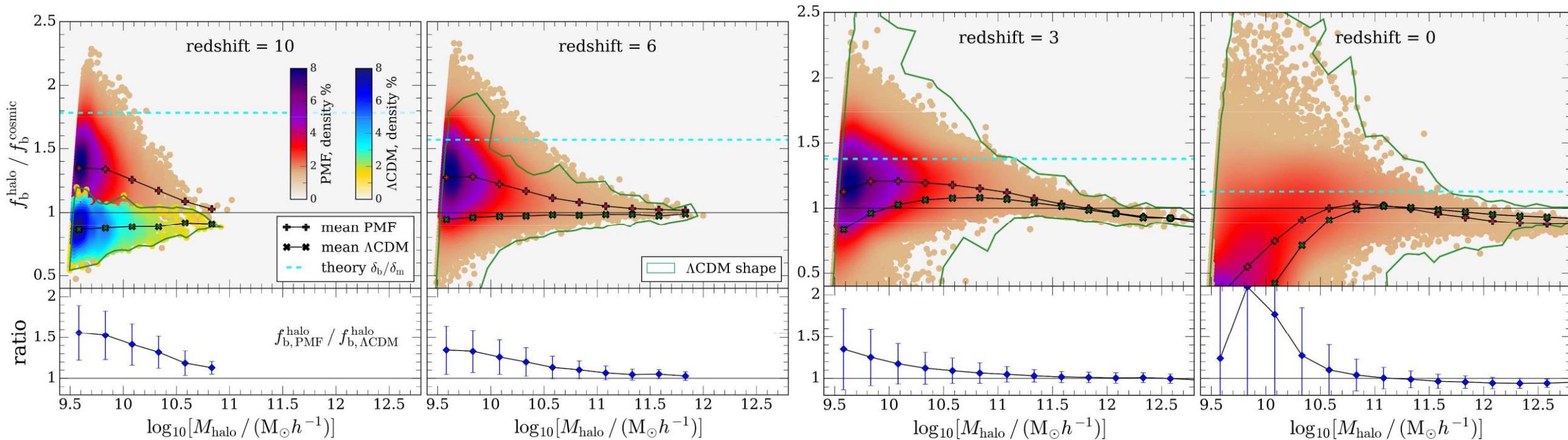


# Simulations



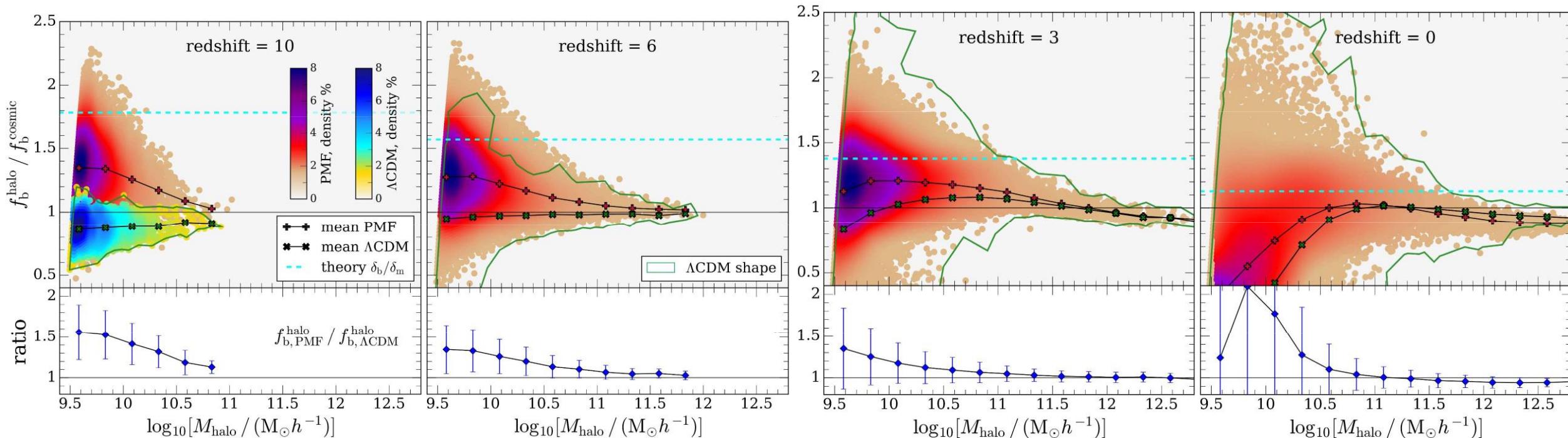
# Baryon fraction in halos: enhanced by PMFs

# Baryon fraction in halos: enhanced by PMFs



Scale invariant 1 nG PMFs

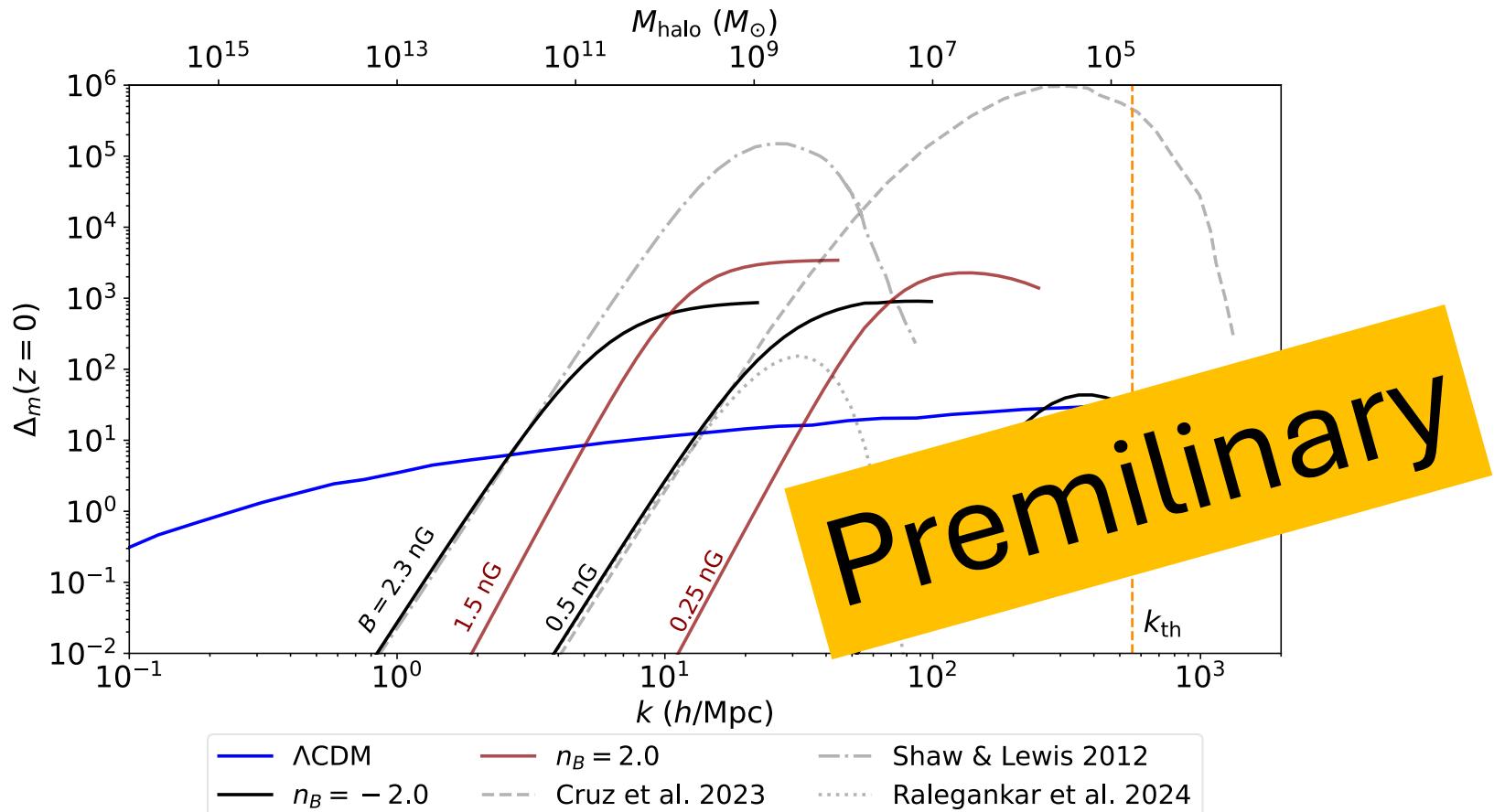
# Baryon fraction in halos: stochastic nature



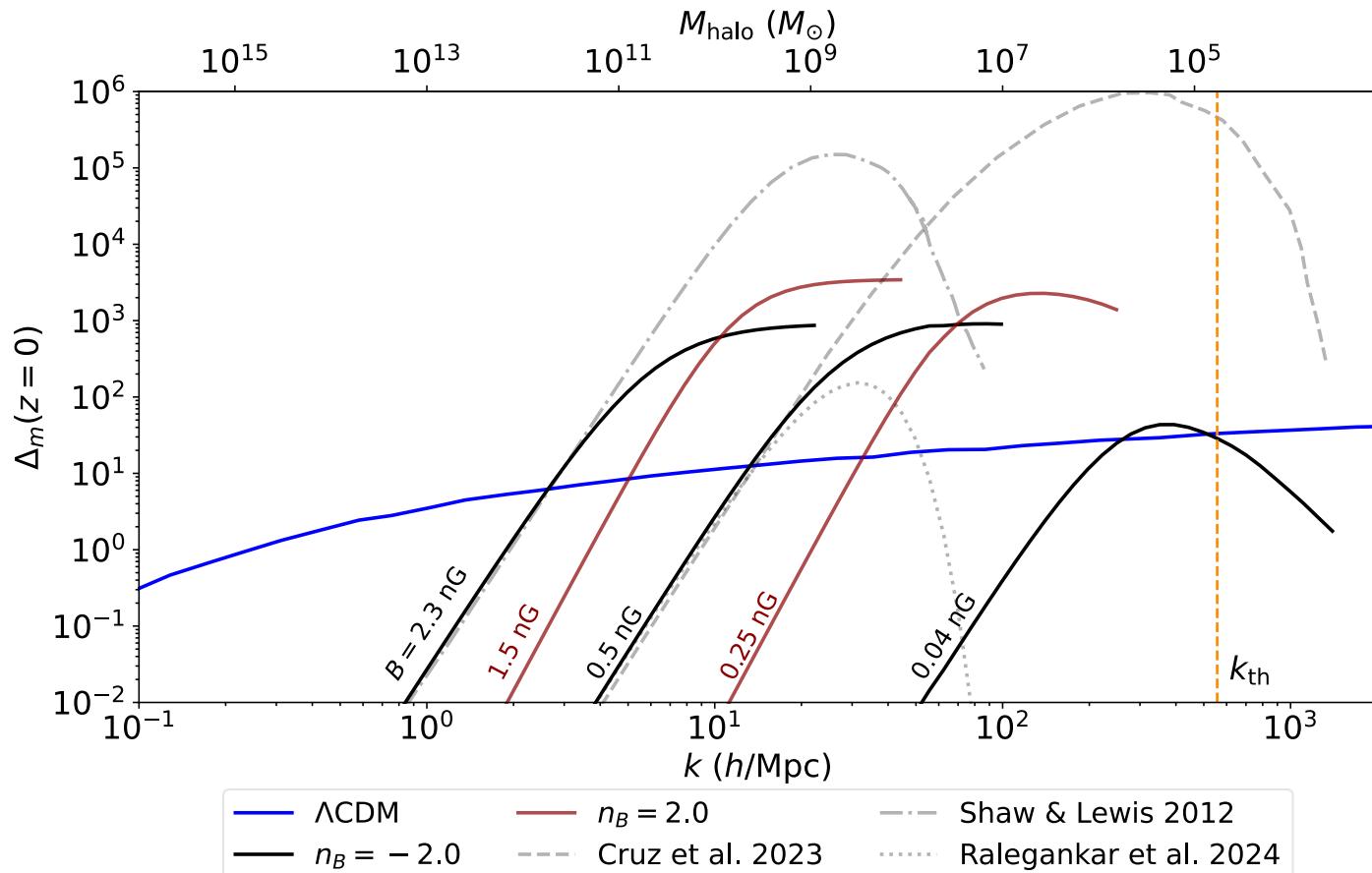
Scale invariant 1 nG PMFs

$$\frac{f_b^{\text{halo}}}{f_b^{\text{cosmic}}} = \frac{\delta_b^{\text{PMF}} + \delta_b^{\Lambda\text{CDM}}}{\delta_m^{\text{PMF}} + \delta_m^{\Lambda\text{CDM}}}$$

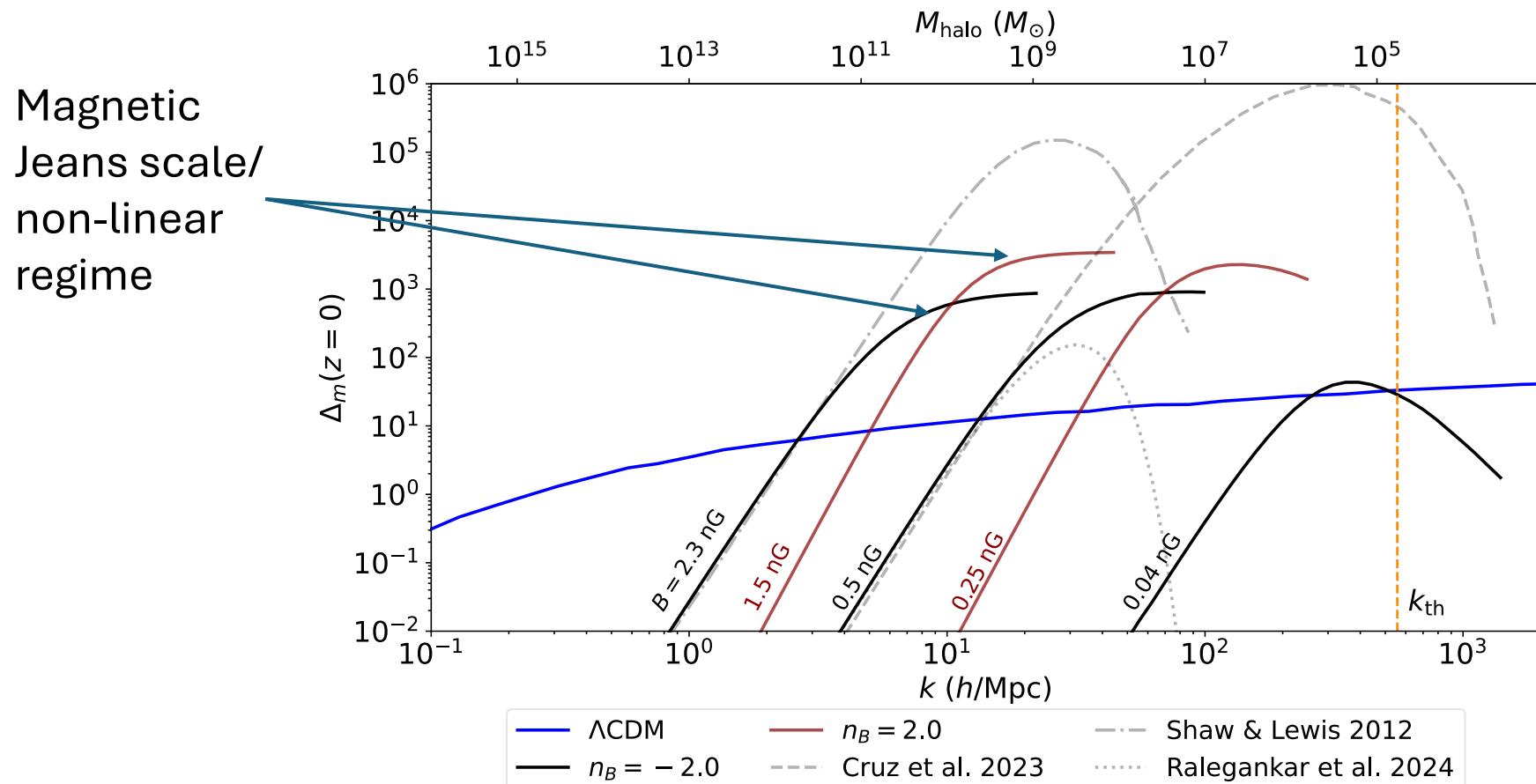
# Enhancement moves to smaller scales with smaller PMF strength



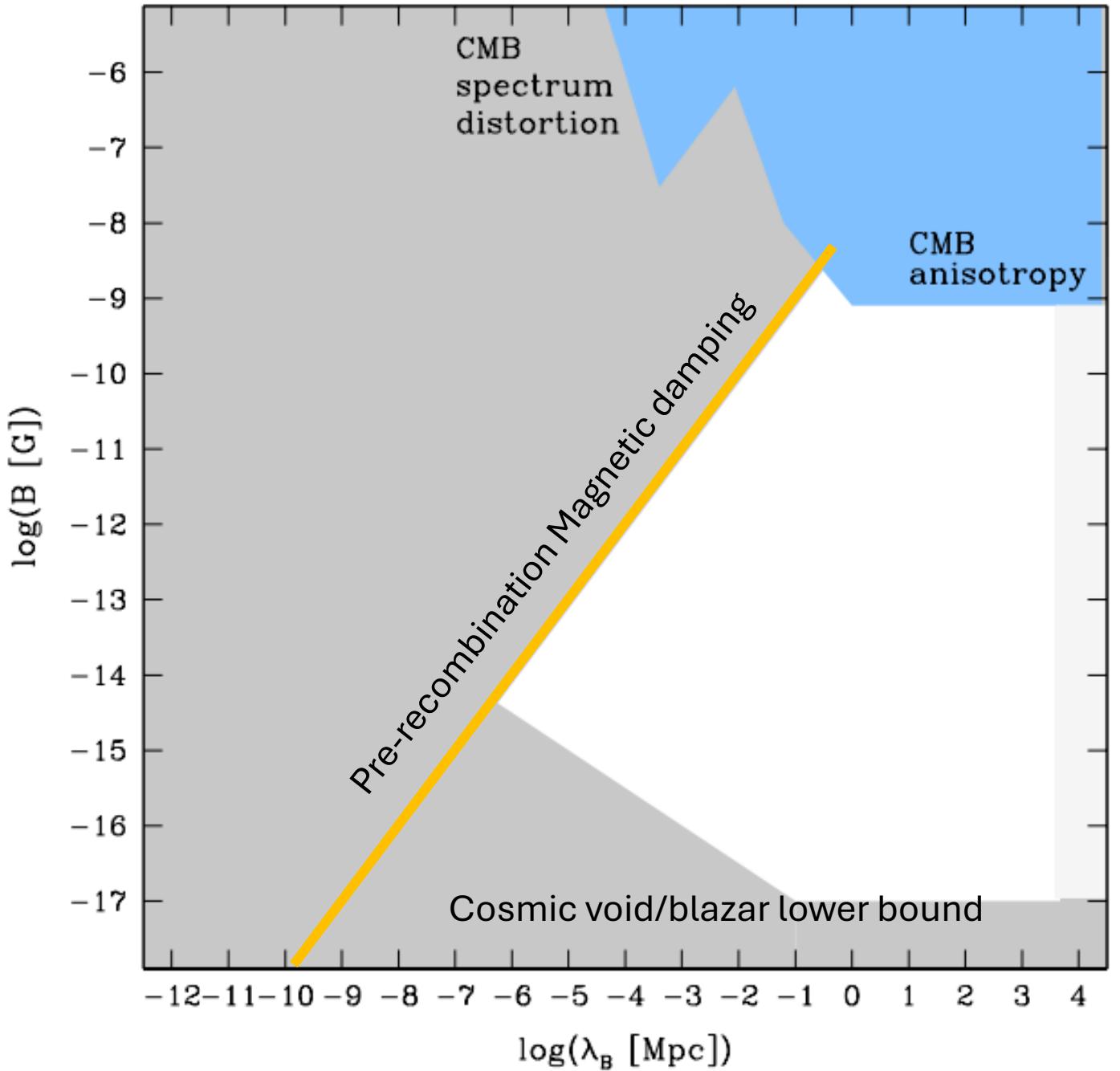
# Enhancement moves to smaller scales with smaller PMF strength



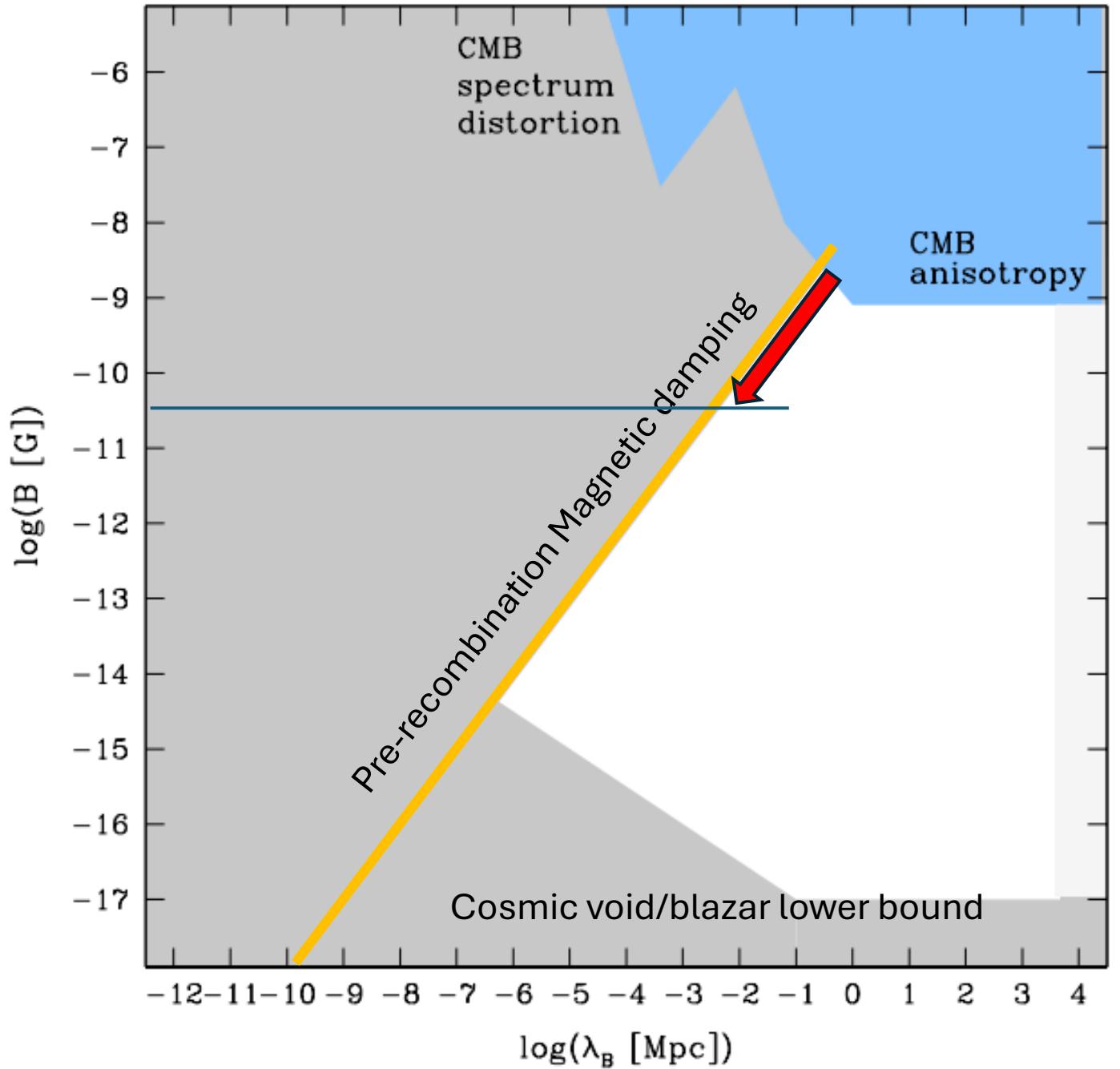
# Enhancement moves to smaller scales with smaller PMF strength



# Implications for PMFs

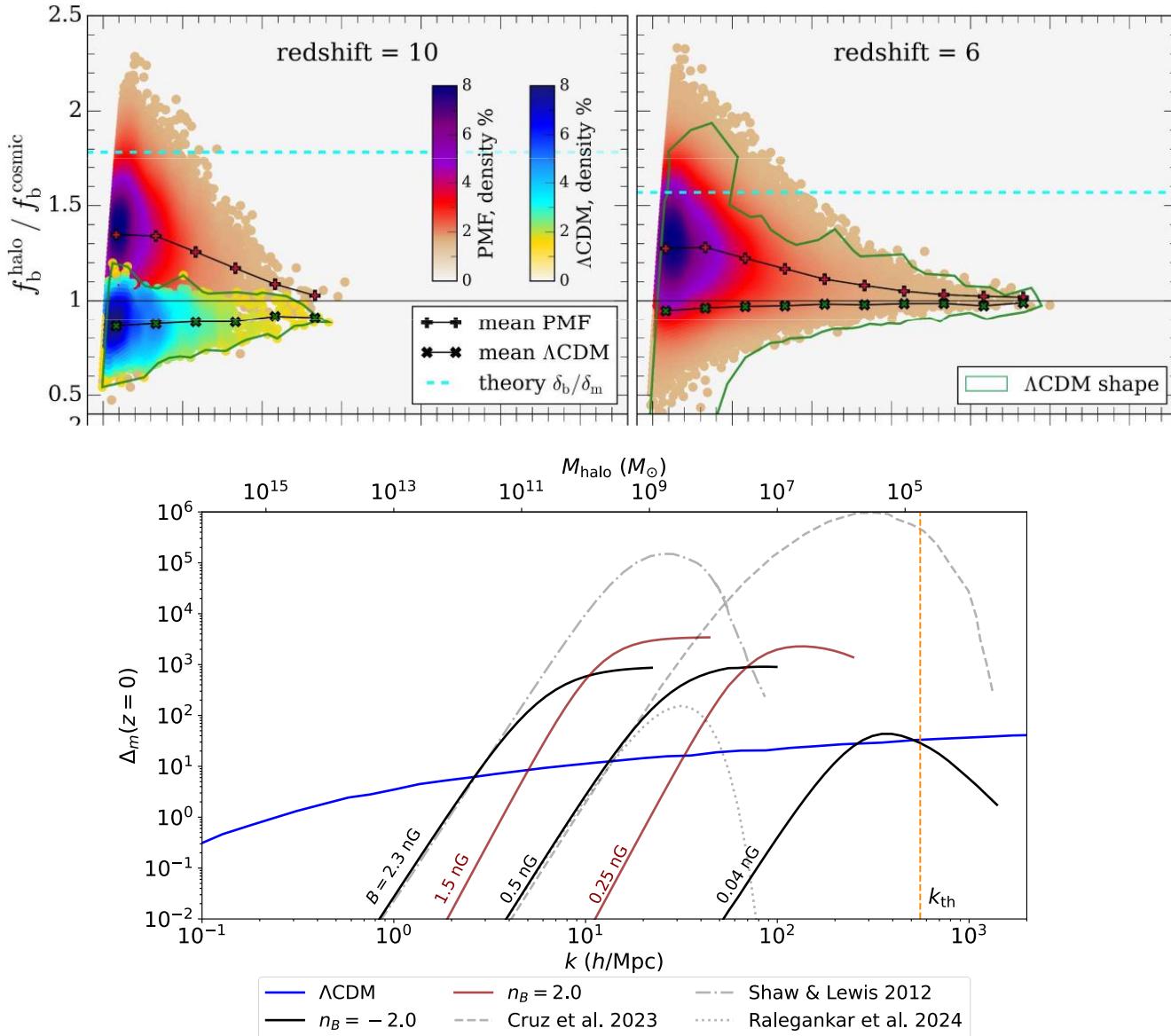


Power spectrum above magnetic jeans scale is sensitive upto 0.05 nG PMFs



# Part 1: summary

- PMFs can enhance baryon fraction apart from enhancing matter power spectrum
- Can affect star formation efficiency, black hole formation etc. Need dedicated MHD sims.
- The final conclusion of enhanced baryon fraction in halos does not depend on MHD.
- Observing high baryon fraction at high redshift will be smoking gun signal for PMFs

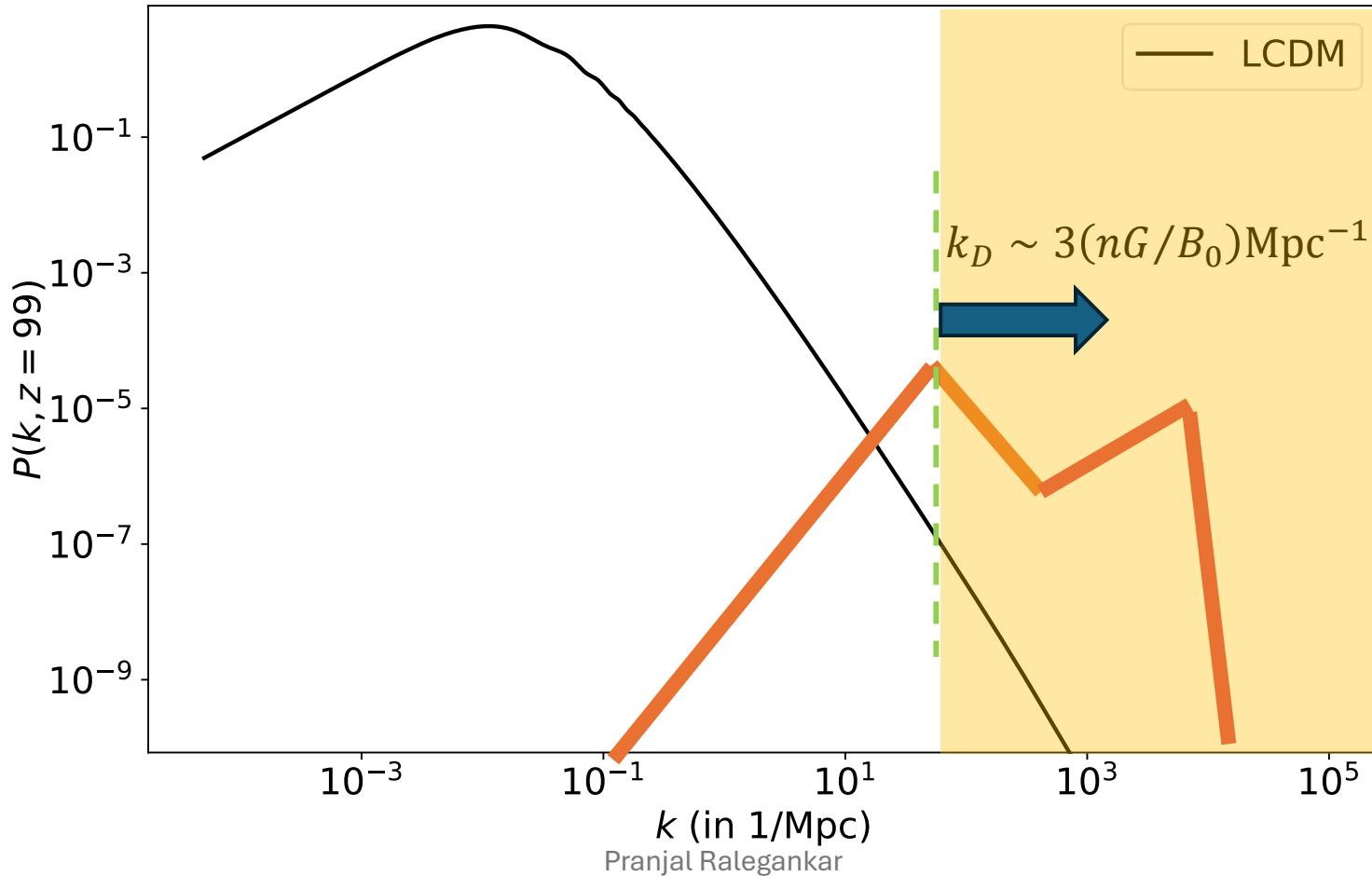


# Part 2

Probing Primordial magnetic fields through  
dark matter minihalos

ARXIV: 2303.11861

# Part 2: Dark matter minihalos below jeans scale



# Pre-recombination Ideal MHD.. With non-linear terms

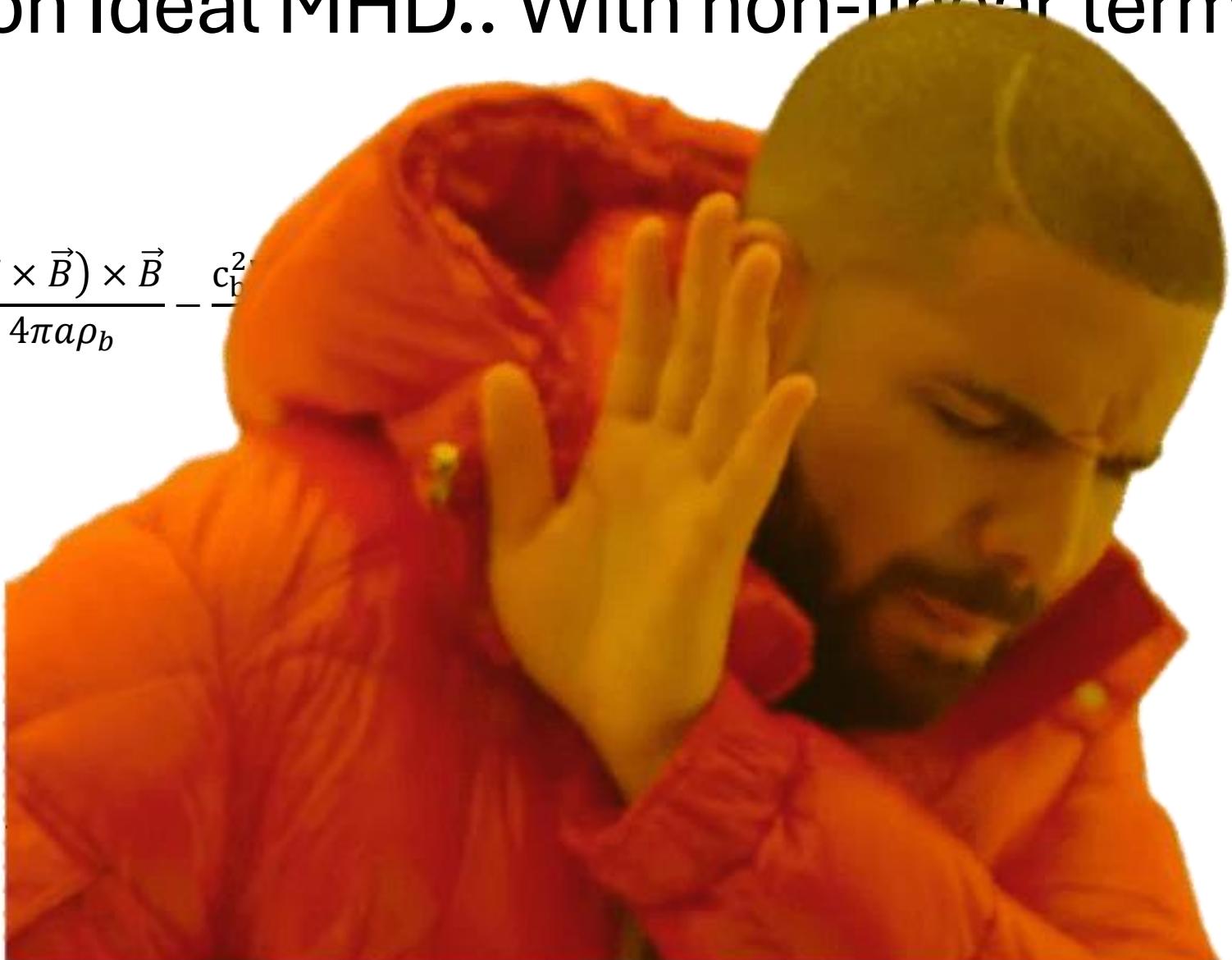
$$\frac{\partial (\vec{B})}{\partial t} = \frac{\nabla \times (\vec{v}_b \times \vec{B})}{a}$$

$$\frac{\partial \vec{v}_b}{\partial t} + (H + \alpha) \vec{v}_b + \frac{(\vec{v}_b \cdot \nabla) \vec{v}_b}{a} = \frac{(\nabla \times \vec{B}) \times \vec{B}}{4\pi a \rho_b} - \frac{c_b^2}{a}$$

$$\frac{\partial \delta_b}{\partial t} = -\frac{\nabla \cdot \vec{v}_b}{a} - \frac{\nabla \cdot (\delta_b \vec{v}_b)}{a}$$

$$\nabla^2 \phi = \frac{a^2}{2M_{Pl}^2} (\rho_b \delta_b + \rho_{DM} \delta_{DM})$$

$$\frac{\partial^2 \delta_{DM}}{\partial a^2} + \left[ \frac{\partial \ln(a^2 H)}{\partial \ln a} + 1 \right] \frac{\partial \delta_{DM}}{\partial a} =$$



# Pre-recombination Ideal MHD.. With non-linear terms

$$\frac{\partial (\vec{B})}{\partial t} = \frac{\nabla \times (\vec{v}_b \times \vec{B})}{a}$$

$$\frac{\partial \vec{v}_b}{\partial t} + (H + \alpha) \vec{v}_b + \frac{(\vec{v}_b \cdot \nabla) \vec{v}_b}{a} = \frac{(\nabla \times \vec{B}) \times \vec{B}}{4\pi a \rho_b} - \frac{c_b^2 \nabla \delta_b}{a} - \frac{\nabla \phi}{a}$$

$$\frac{\partial \delta_b}{\partial t} = - \frac{\nabla \cdot \vec{v}_b}{a} - \frac{\nabla \cdot (\delta_b \vec{v}_b)}{a}$$

$$\nabla^2 \phi = \frac{a^2}{2M_{Pl}^2} (\rho_b \delta_b + \rho_{DM} \delta_{DM})$$

$$\frac{\partial^2 \delta_{DM}}{\partial a^2} + \left[ \frac{\partial \ln(a^2 H)}{\partial \ln a} + 1 \right] \frac{\partial \delta_{DM}}{\partial a} = \frac{\nabla^2 \phi}{(a^2 H)^2}$$

# Pre-recombination Ideal MHD: laminar flow due to photon drag

$$\frac{\partial (\vec{B})}{\partial t} = \frac{\nabla \times (\vec{v}_b \times \vec{B})}{a}$$

$$\frac{\partial \vec{v}_b}{\partial t} + (H + \alpha) \vec{v}_b + \frac{(\vec{v}_b \cdot \nabla) \vec{v}_b}{a} = \frac{(\nabla \times \vec{B}) \times \vec{B}}{4\pi a \rho_b} - \frac{c_b^2 \nabla \delta_b}{a} - \frac{\nabla \phi}{a}$$

$$\frac{\partial \delta_b}{\partial t} = -\frac{\nabla \cdot \vec{v}_b}{a} - \frac{\nabla \cdot (\delta_b \vec{v}_b)}{a}$$

$$\nabla^2 \phi = \frac{a^2}{2M_{Pl}^2} (\rho_b \delta_b + \rho_{DM} \delta_{DM})$$

$$\frac{\partial^2 \delta_{DM}}{\partial a^2} + \left[ \frac{\partial \ln(a^2 H)}{\partial \ln a} + 1 \right] \frac{\partial \delta_{DM}}{\partial a} = \frac{\nabla^2 \phi}{(a^2 H)^2}$$

# Can analytically solve MHD eqs: viscous damping

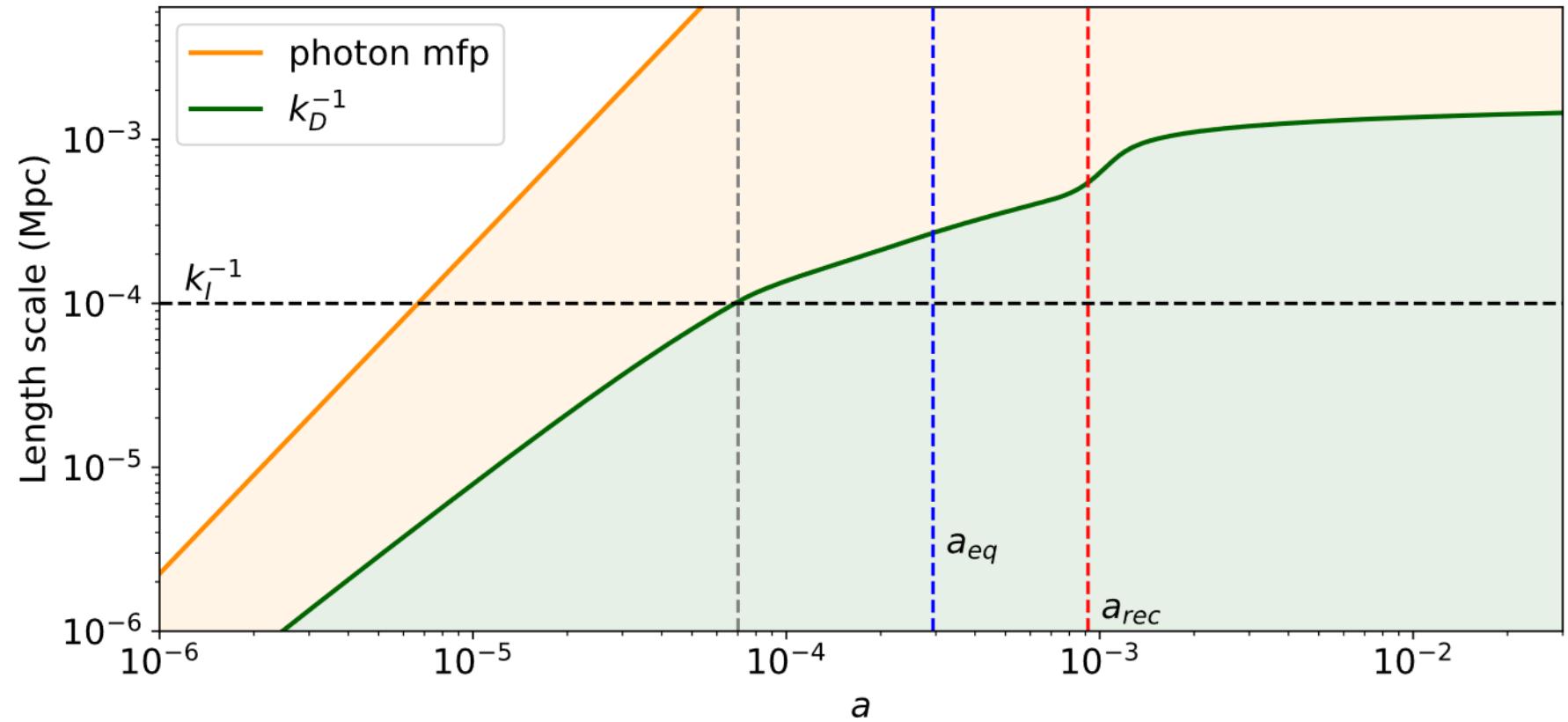
$$P_B(k, t) = P_B(k, t_I) e^{-\frac{k^2}{k_D^2}}$$

$$k_D^{-1}(a) \sim \tau v_b$$

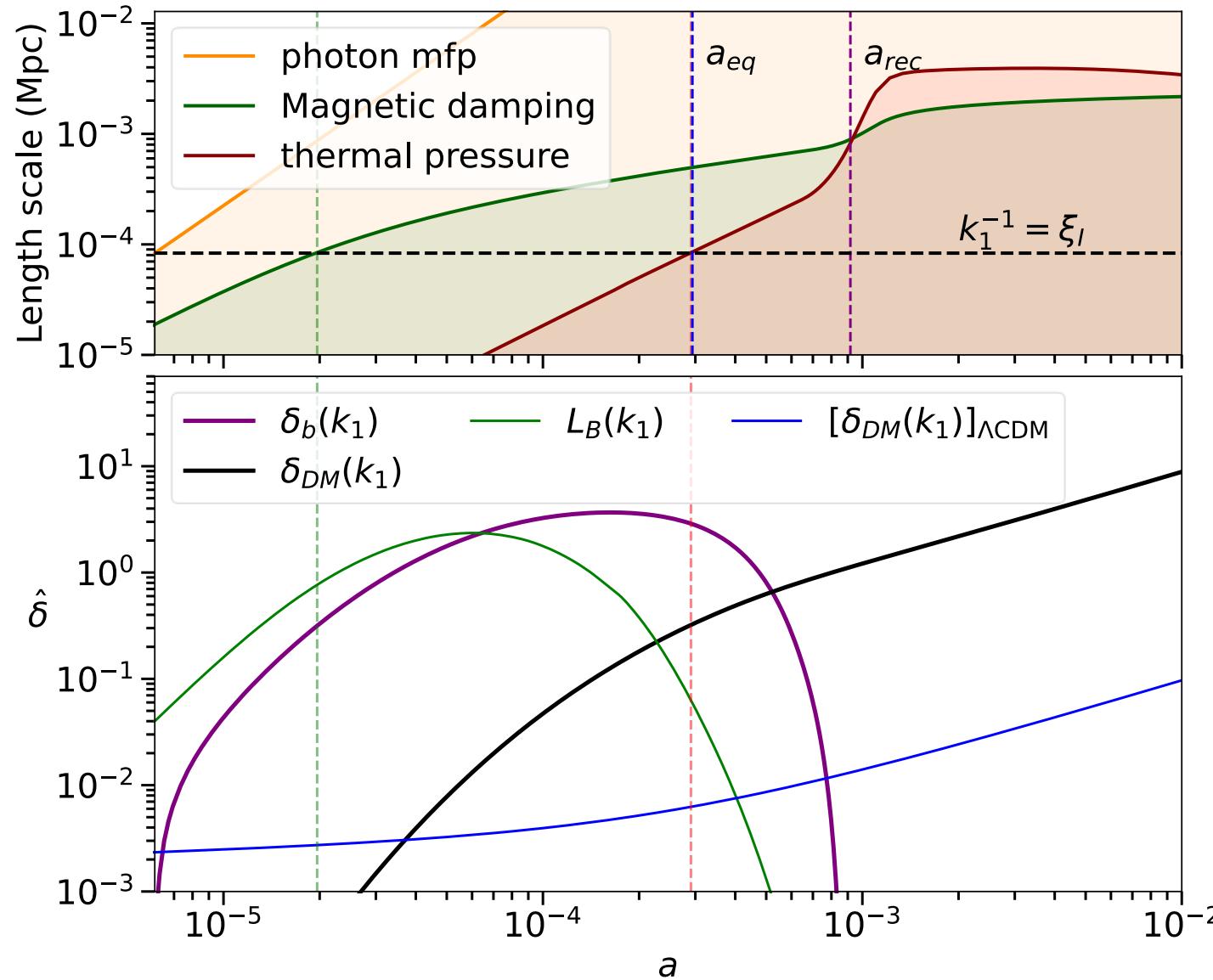
# magnetic damping scale Evolution

$$P_B(k, t) = P_B(k, t_I) e^{-\frac{k^2}{k_D^2}}$$

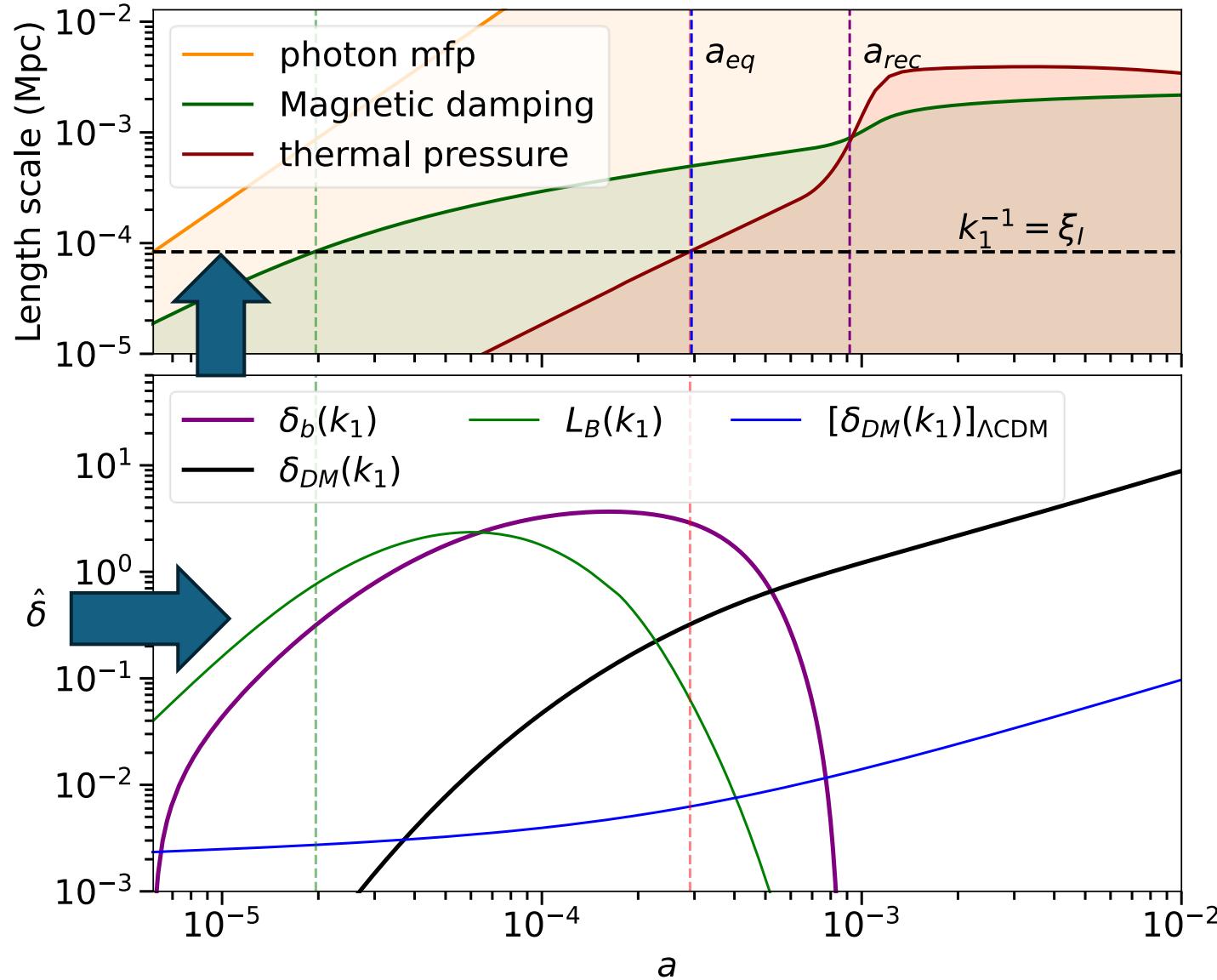
$$k_D^{-1}(a) \sim \tau v_b$$



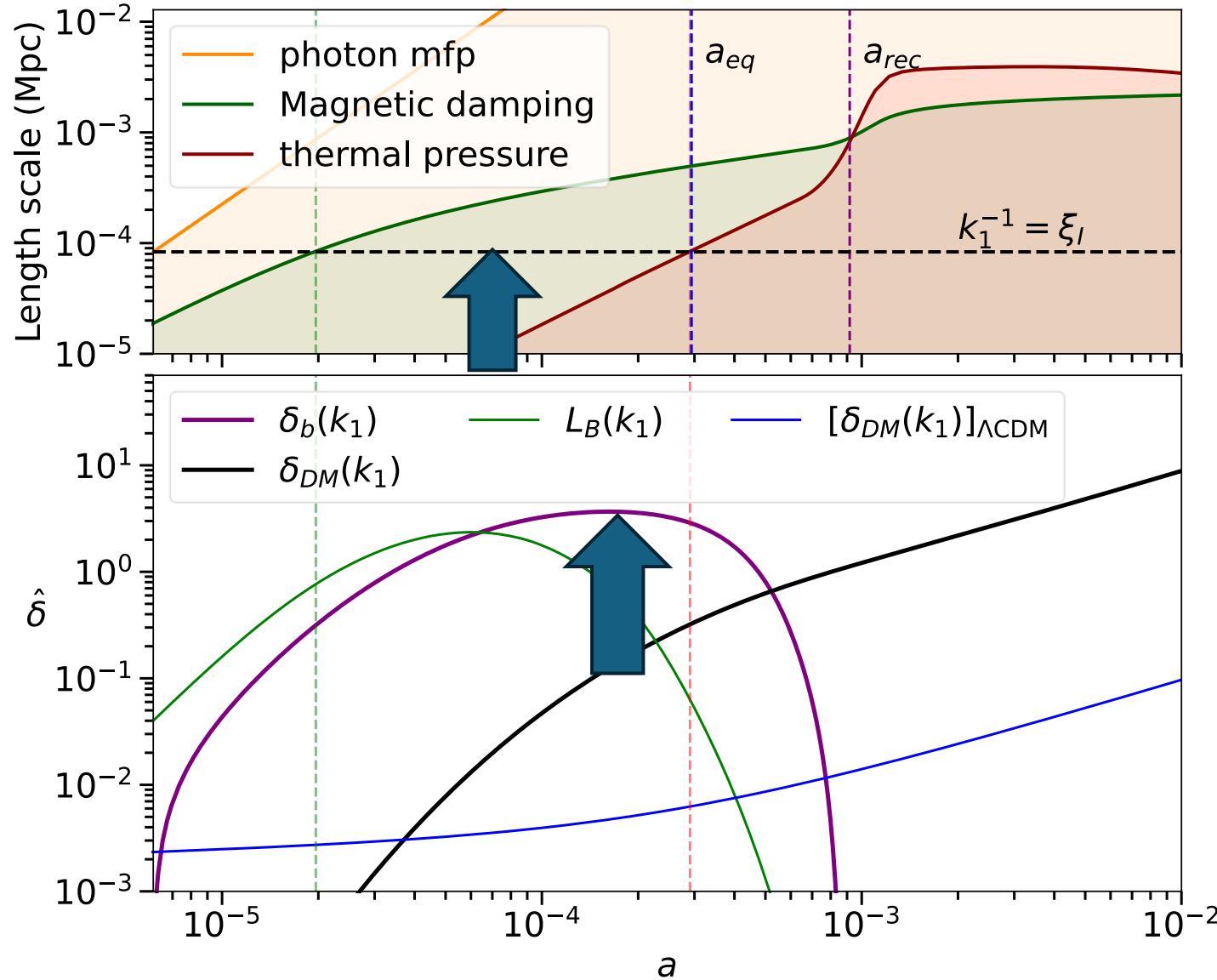
# Perturbation evolution plot



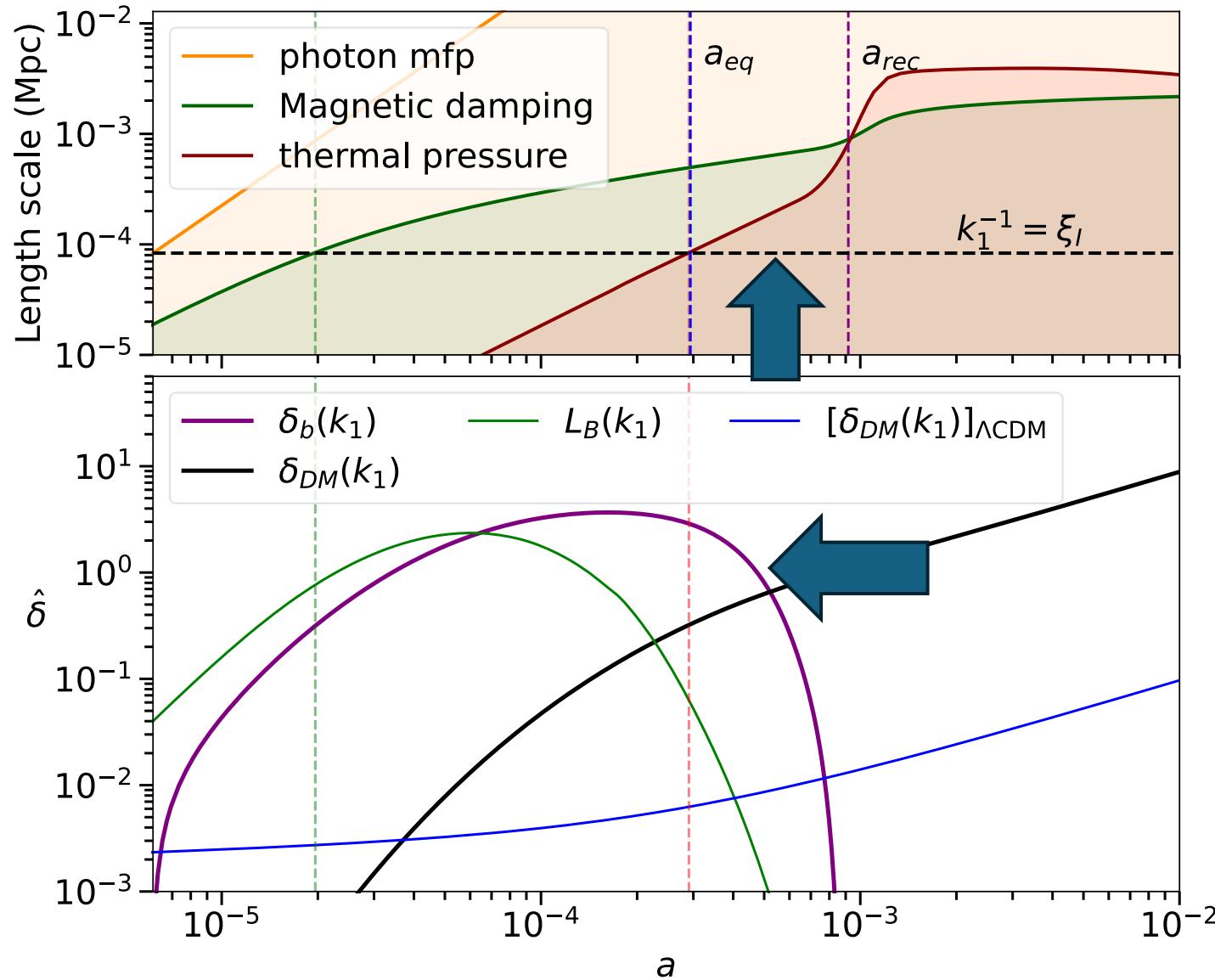
# Lorentz force enhances baryon perturbations for modes outside $k_D^{-1}$



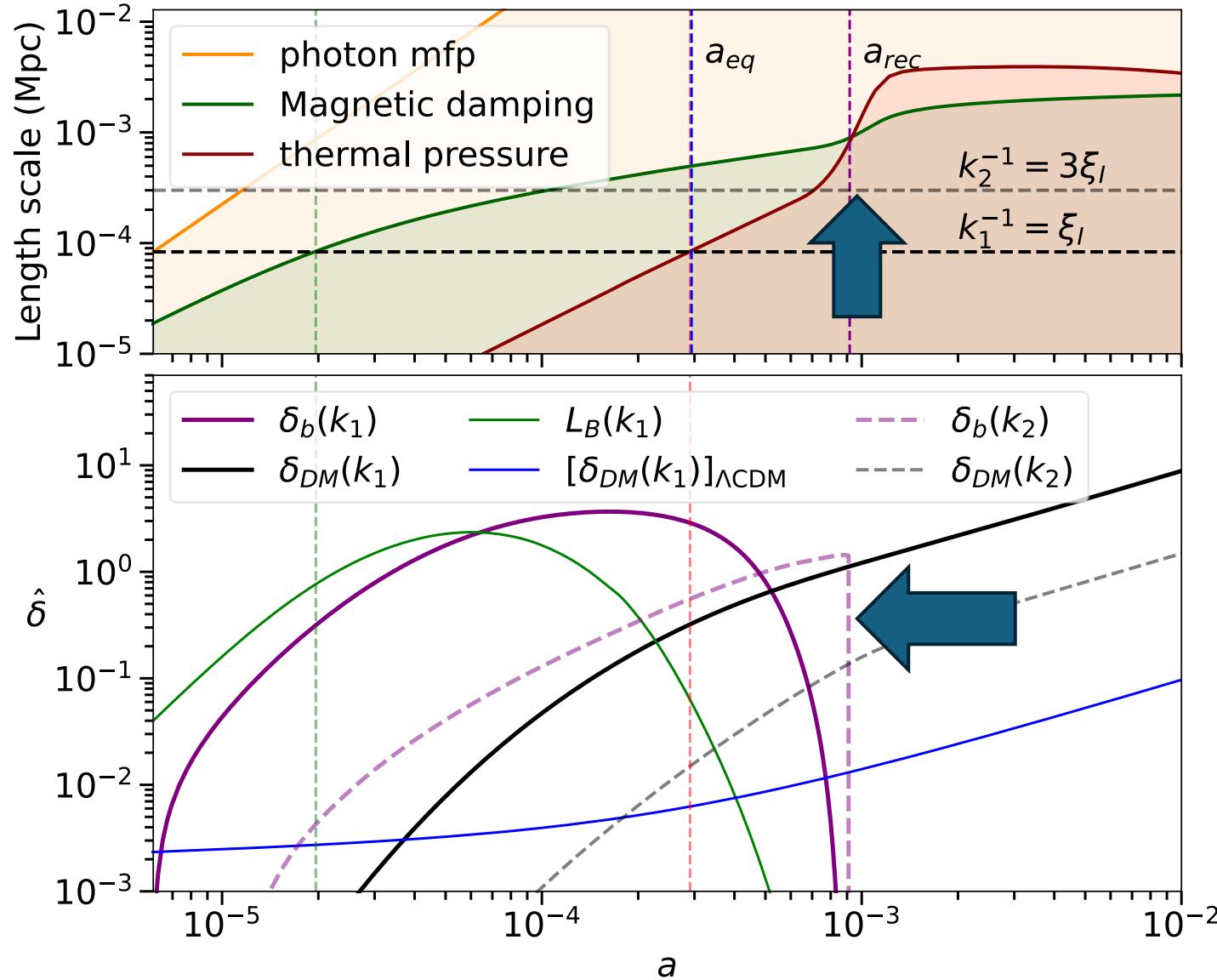
# baryon perturbations asymptote once mode enters $k_D^{-1}$



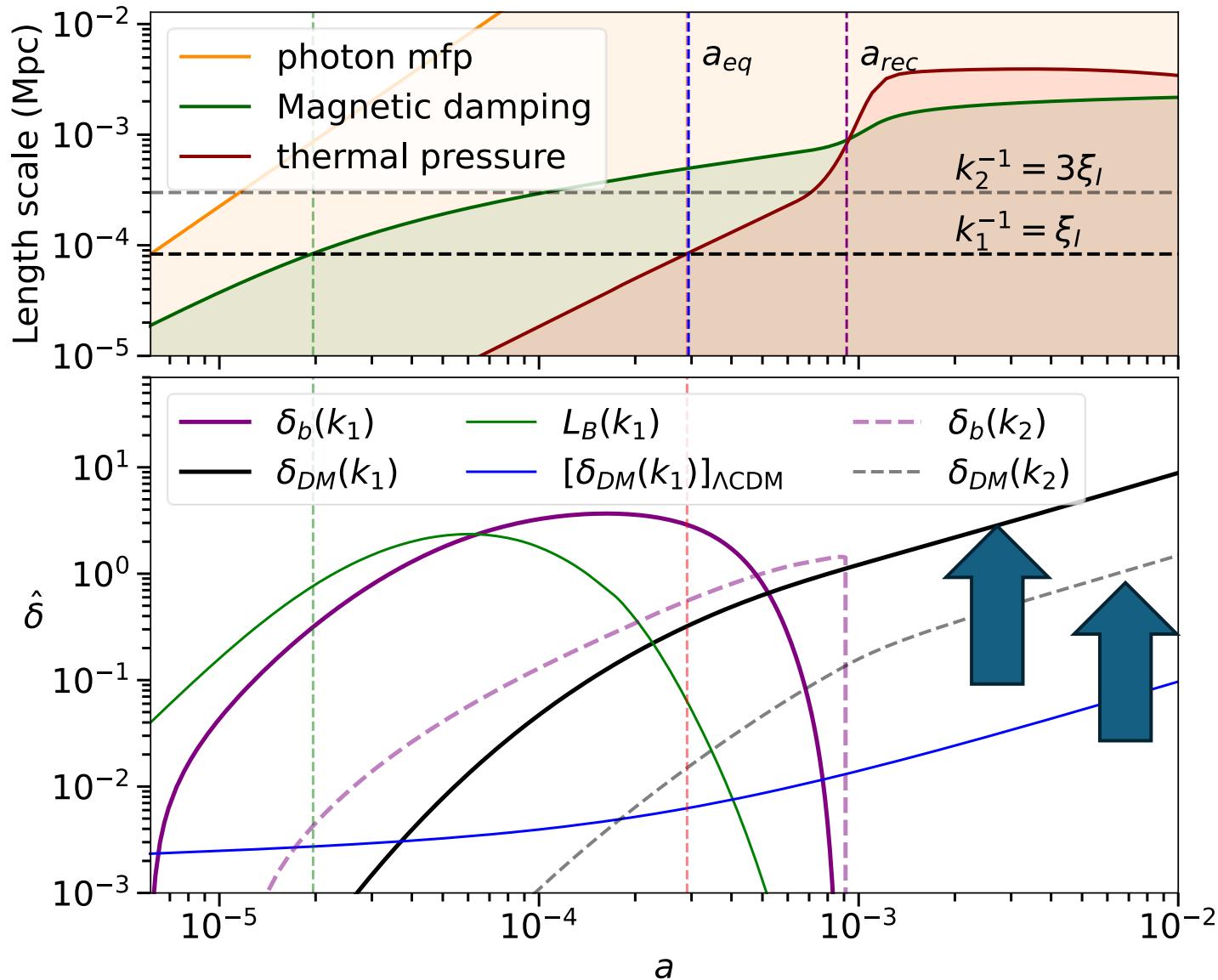
# baryon perturbations damped by thermal pressure



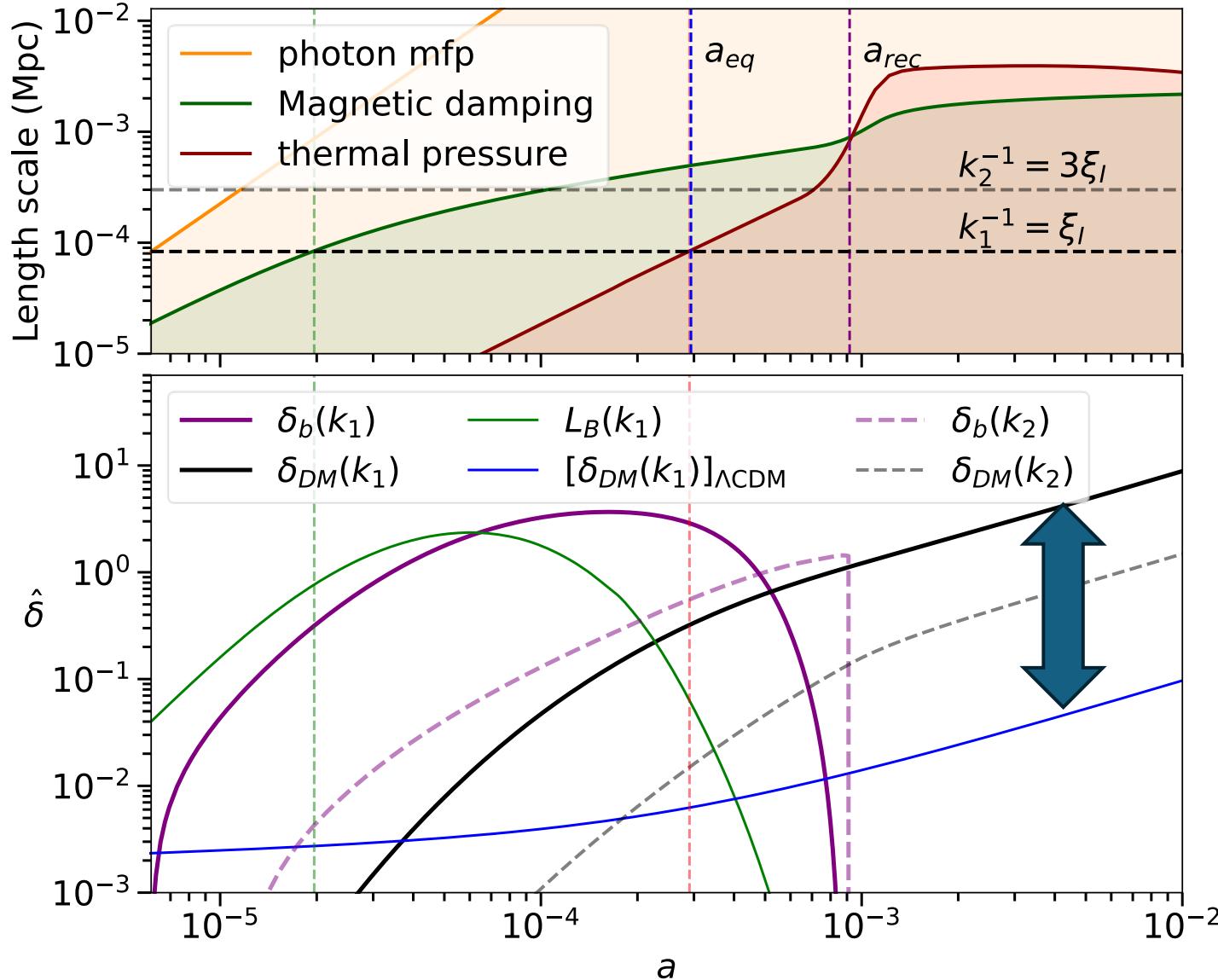
# baryon perturbations damped by turbulence at recombination



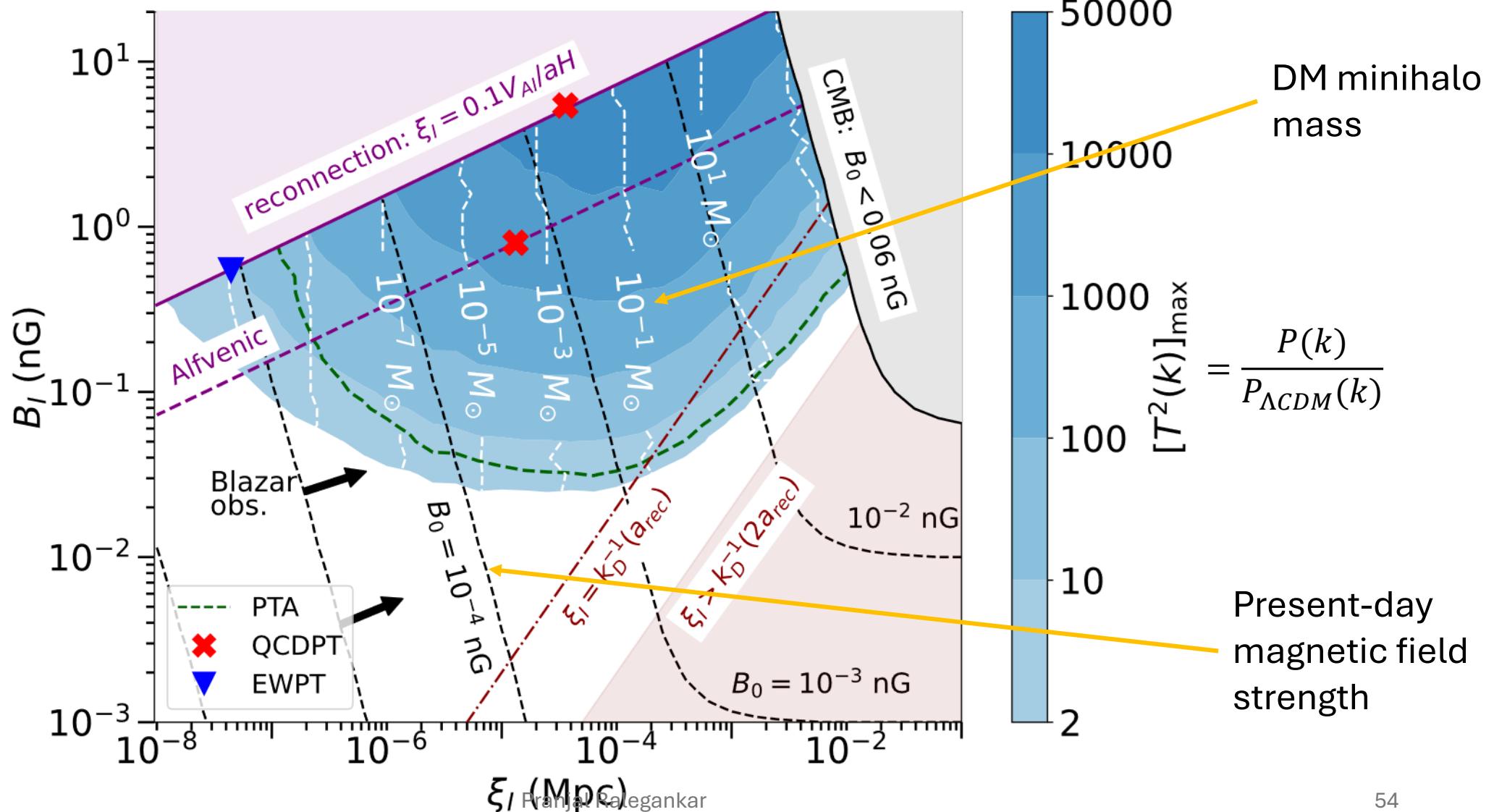
# Dark matter perturbations continues to grow!



# Dark matter perturbations enhanced by orders of magnitude compared to $\Lambda$ CDM

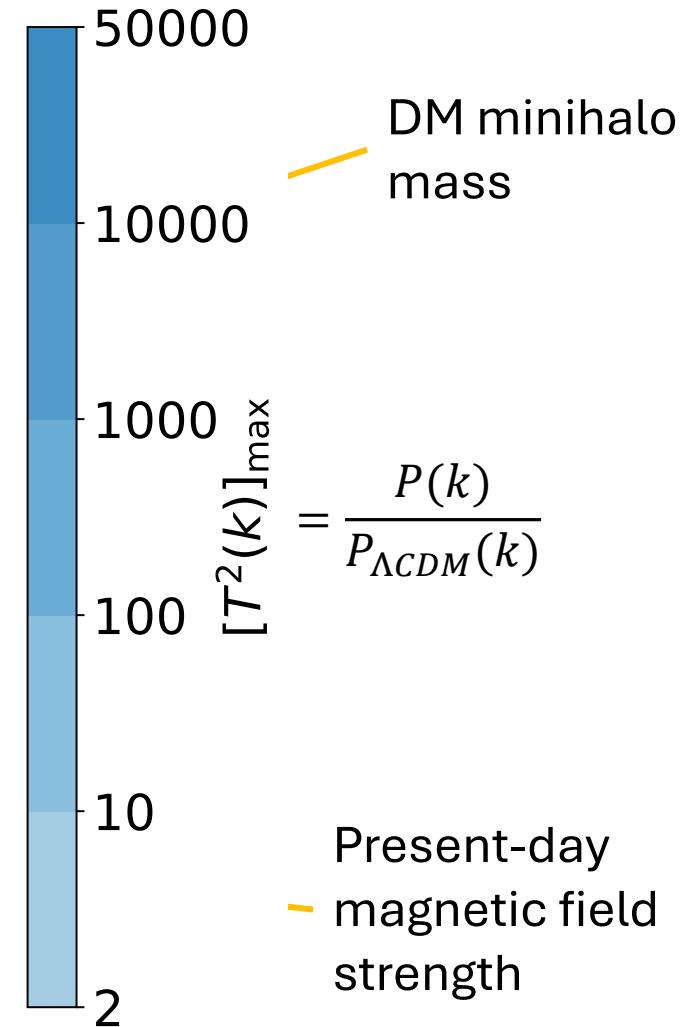
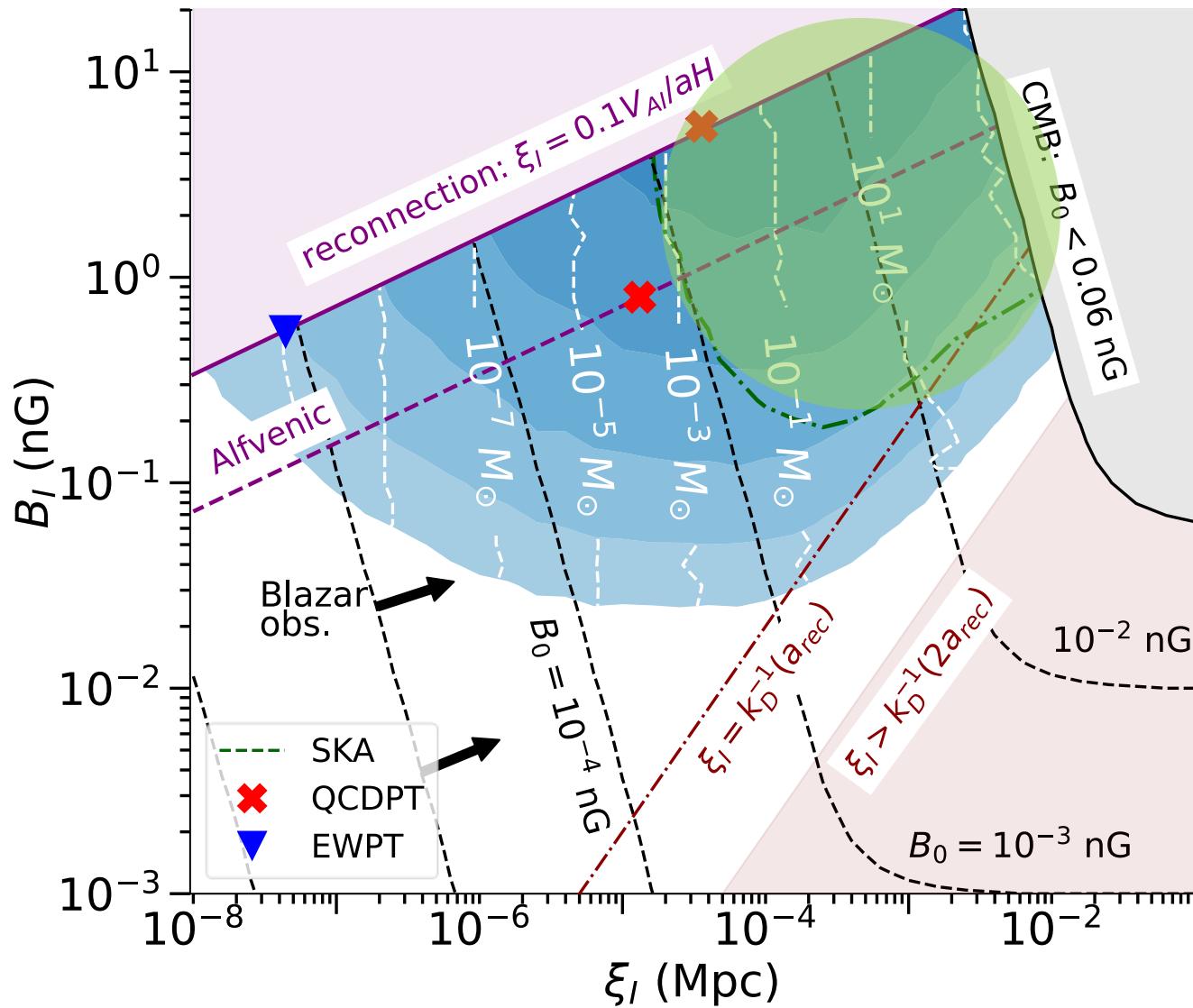


# Parameter Space with Enhanced Power on Small scales



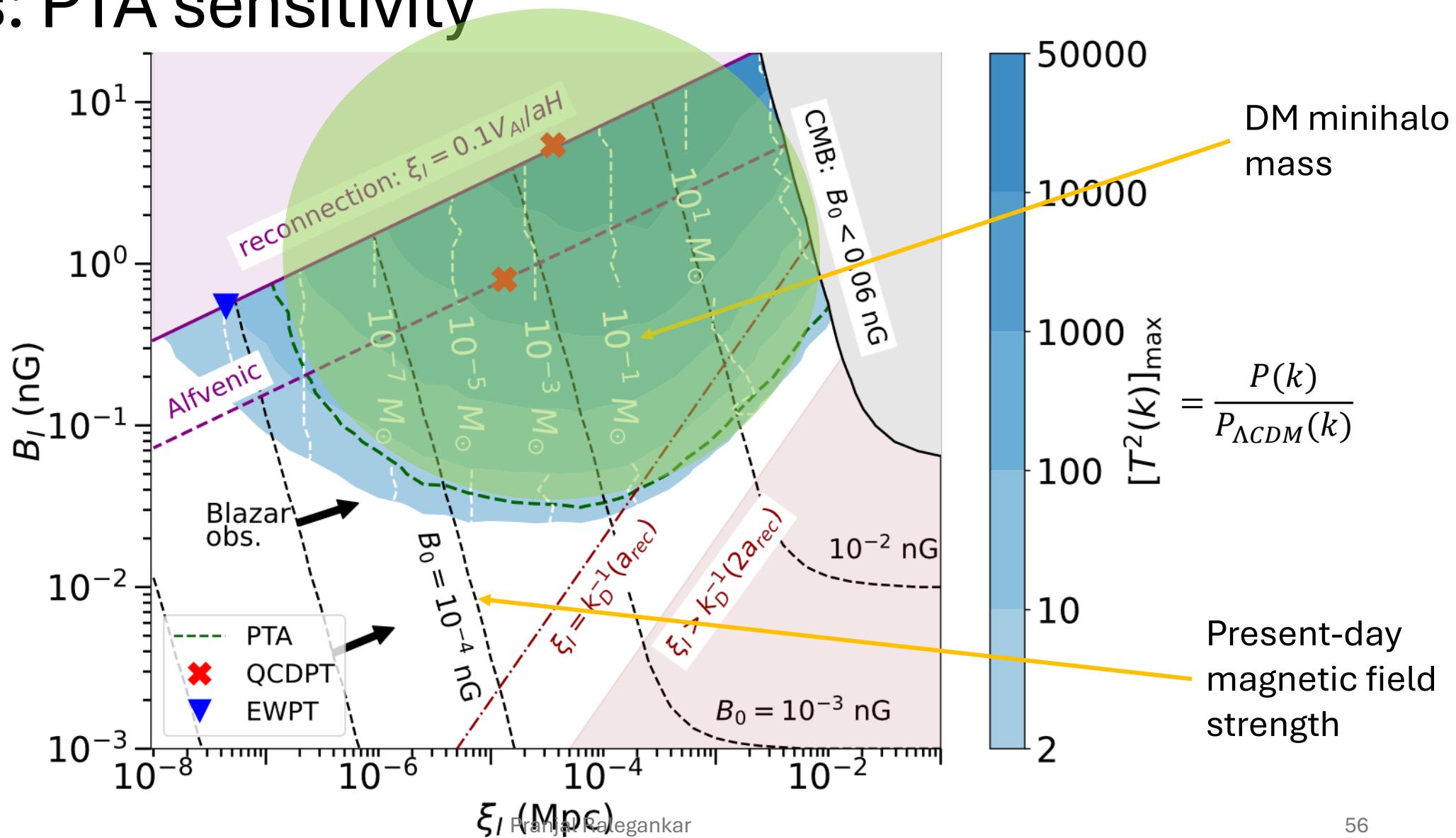
# Parameter Space with Enhanced Power on Small scales: THEIA SKA sensitivity

Subscript  $I$  refers to the time at the beginning of laminar flow regime

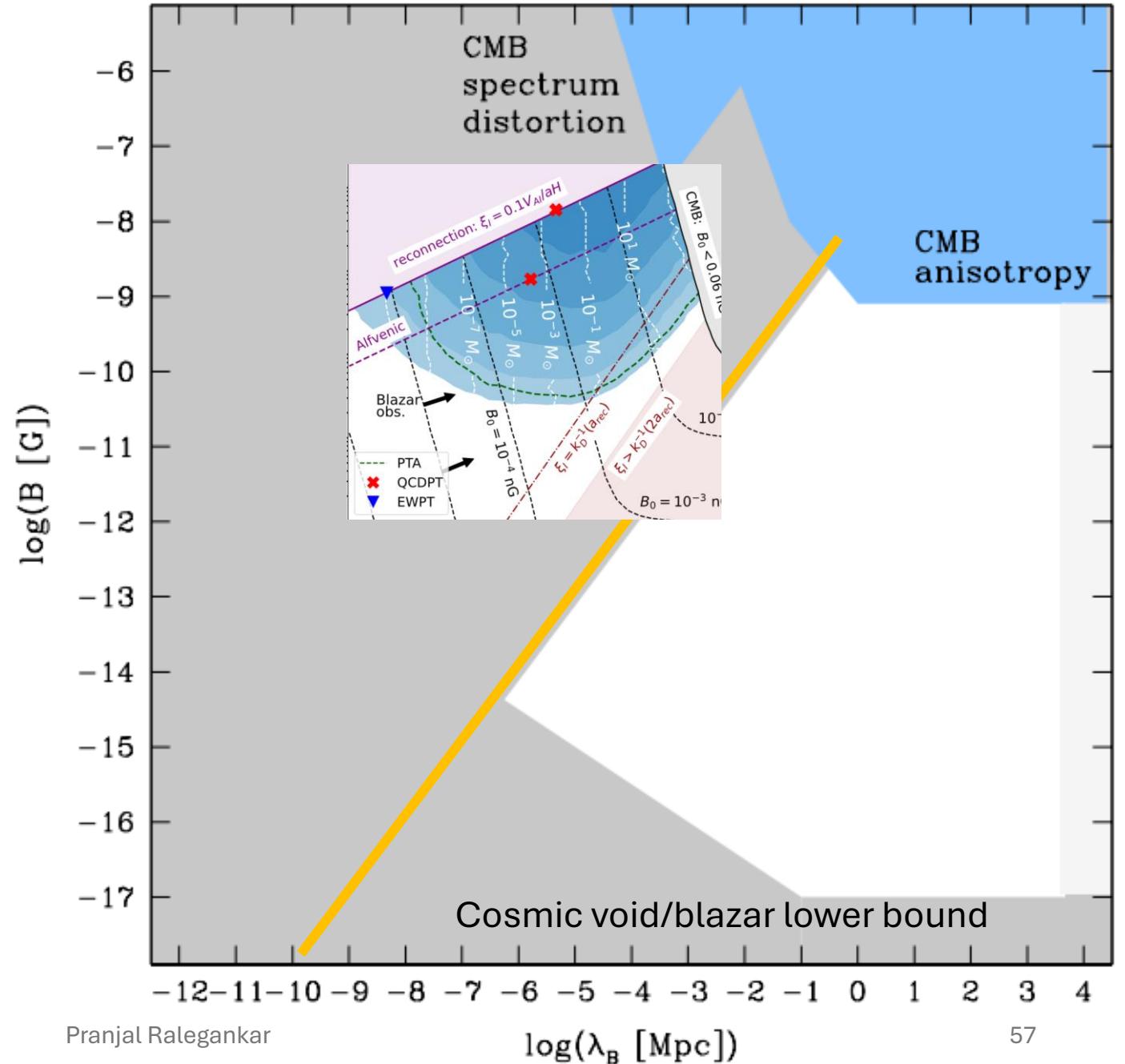


# Parameter Space with Enhanced Power on Small scales: PTA sensitivity

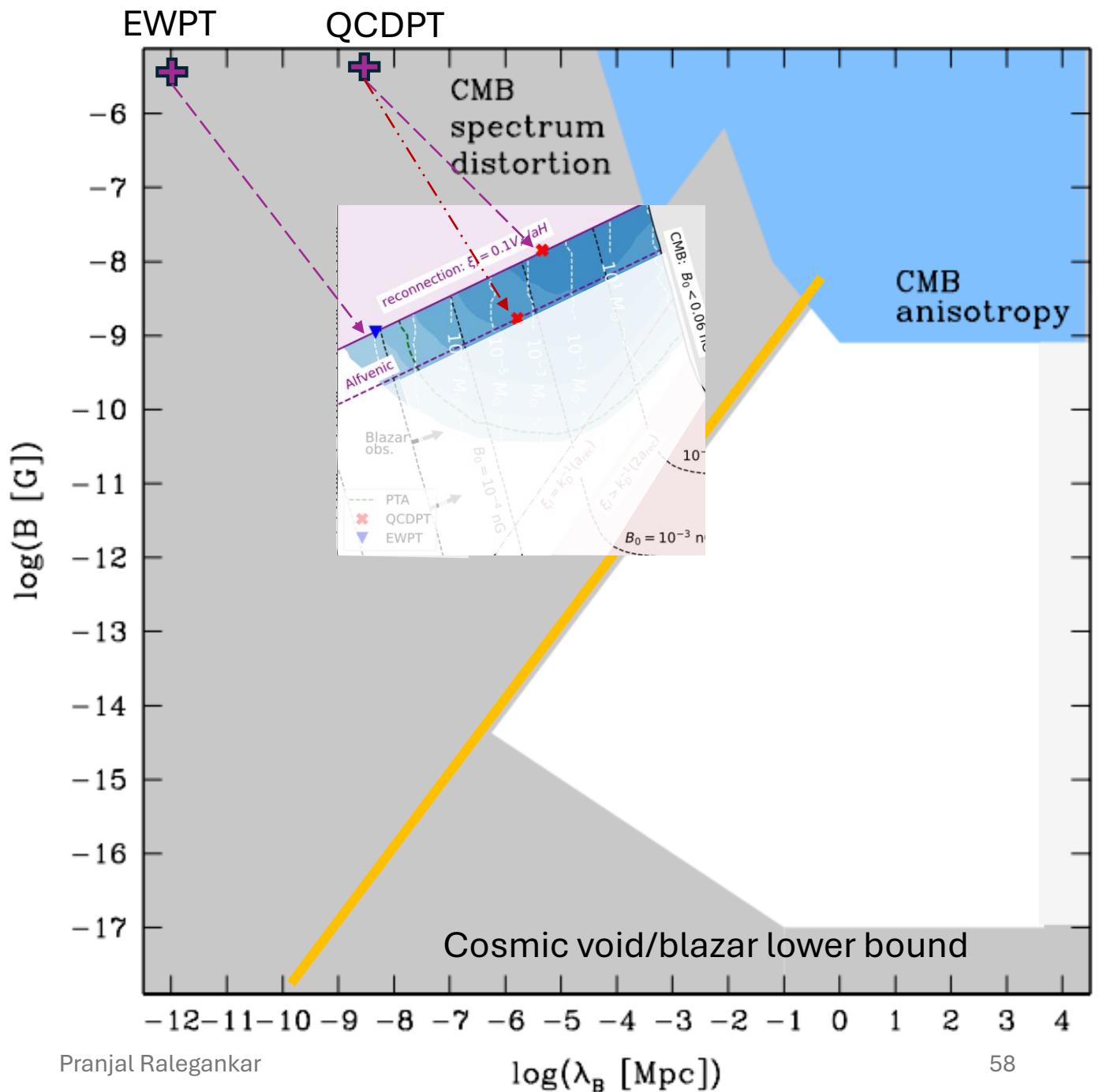
Subscript  $I$  refers to the time at the beginning of laminar flow regime



# Minihalos from causally generated PMFs

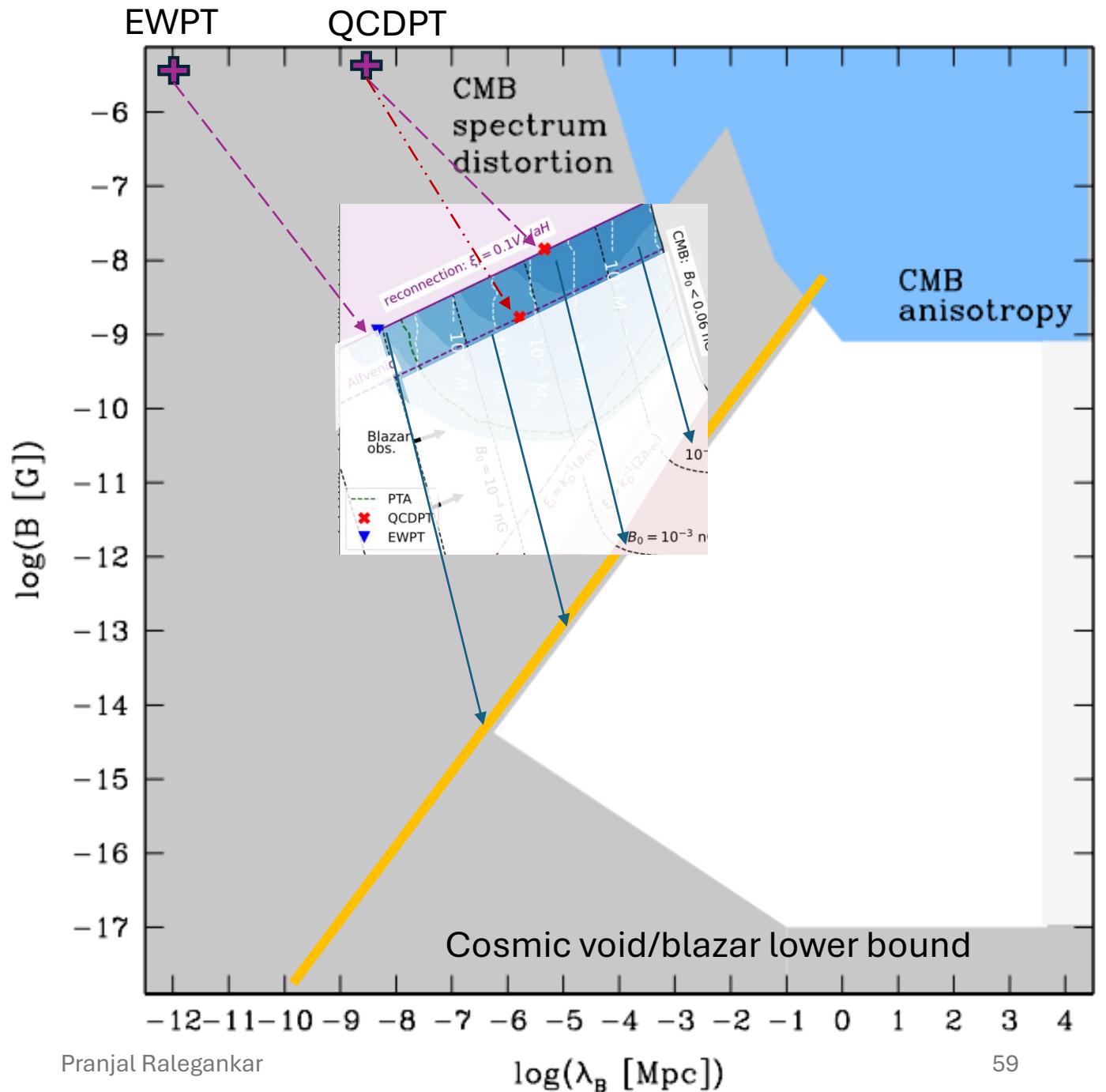


# Minihalos from causally generated PMFs



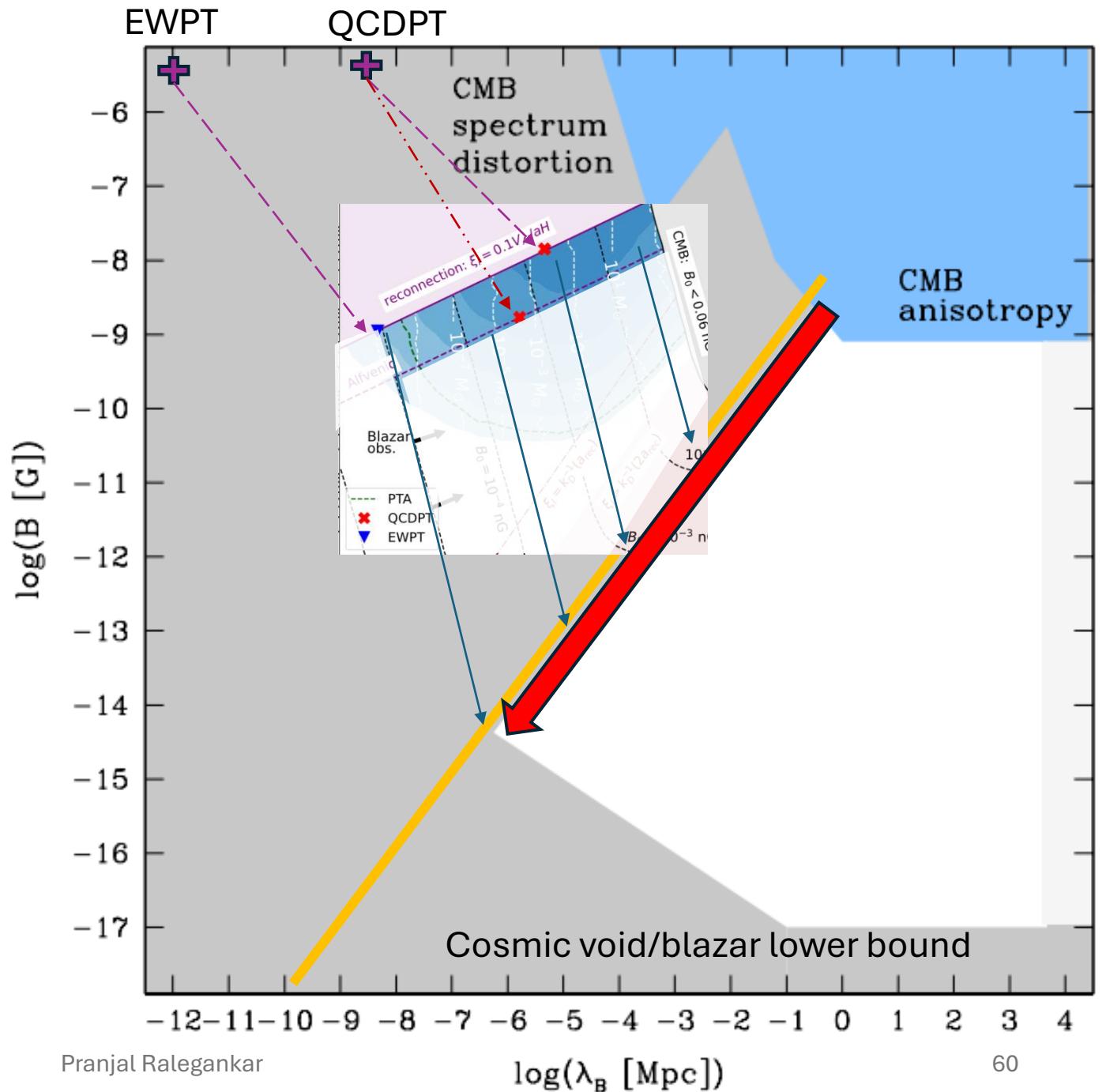
# PMFs to explain cosmic void observations

Assuming Bachelor spectrum!



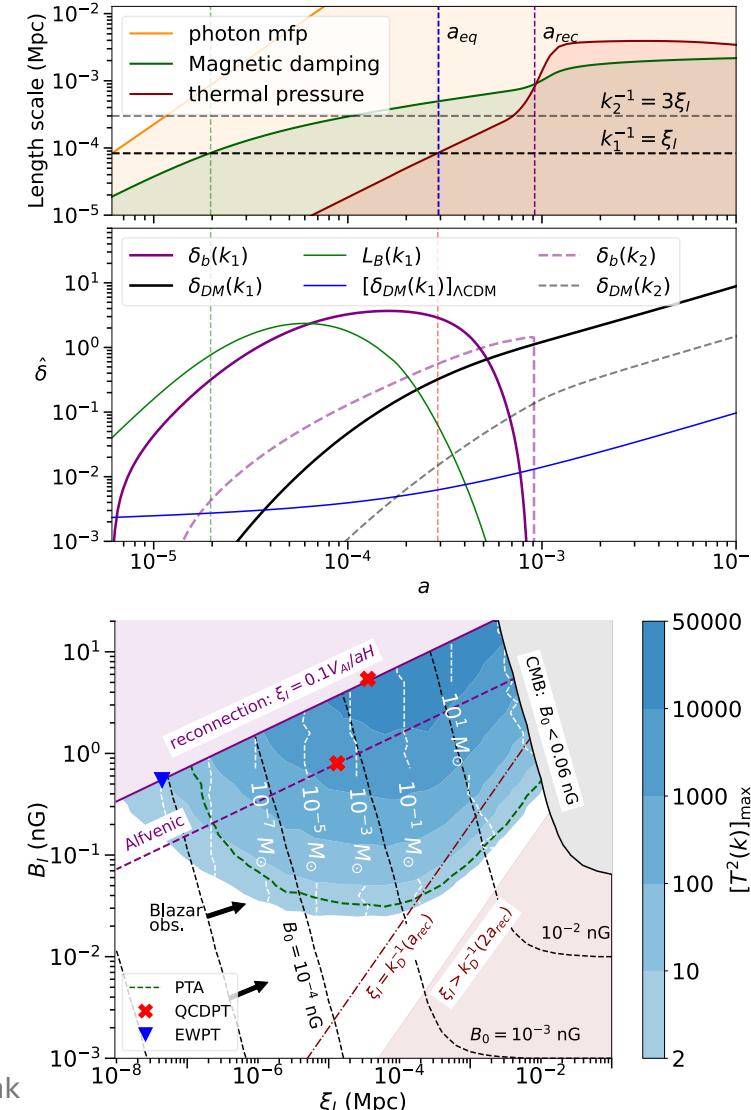
# Universe Maybe filled with dark matter minihalos!!

Assuming Bachelor spectrum!



# Part 2: Summary and Concluding remarks

- Magnetic fields can enhance power on small scale dark matter distribution gravitationally.
- PTA/GAIA detection of DM minihalos can provide best probe of primordial magnetic fields
- PMFs resolving Hubble tension likely produce minihalos
- Ironic: how invisible dark matter can help look for visible entity: magnetic fields



# Backup

# Back to power spectrum

